

## Mahdollisesti hyödyllisiä tietoja / potentially useful information

$$k_B = 1.3805 \times 10^{-23} \text{ J/K} , \quad R = k_B N_A = 8.3143 \text{ J/(mol K)} , \quad N_A = 6.022 \times 10^{23} \text{ 1/mol}$$

$$k_B \times 11600 \text{ K} \approx 1 \text{ eV} , \quad 0^\circ\text{C} = 273.15 \text{ K} , \quad 1 \text{ atm} = 1.013 \times 10^5 \text{ Pa} , \quad g = 9.82 \text{ m/s}^2 , \quad c = 2.998 \times 10^8 \text{ m/s}$$

$$\hbar = 1.054 \times 10^{-34} \text{ Js} , \quad 1 \text{ J} = 1.602 \times 10^{-19} \text{ eV} , \quad m_e c^2 = 511 \text{ keV} \quad 1u = 1.66 \times 10^{-27} \text{ kg}$$

$$dU = \delta Q + \delta W^{\text{rev}} = TdS - PdV , \quad dU = TdS - PdV + \mu dN$$

$$F = U - TS , \quad G = U - TS + PV , \quad H = U + PV , \quad \Omega = U - TS - \mu N = -PV$$

$$S = k_B \ln \Omega , \quad F = -k_B T \ln Z , \quad U = -\frac{\partial}{\partial \beta} \ln Z , \quad \ln(n!) \approx n \ln n - n , \quad \binom{N}{n} \equiv \frac{N!}{n!(N-n)!}$$

$$C_V = T \left( \frac{\partial S}{\partial T} \right)_{V,N} = \left( \frac{\partial U}{\partial T} \right)_{V,N} , \quad C_P = T \left( \frac{\partial S}{\partial T} \right)_{P,N} = \left( \frac{\partial H}{\partial T} \right)_{P,N} , \quad \kappa_T = -\frac{1}{V} \left( \frac{\partial V}{\partial P} \right)_{T,N} , \quad \kappa_S = -\frac{1}{V} \left( \frac{\partial V}{\partial P} \right)_{S,N}$$

$$\left( \frac{\partial x}{\partial y} \right)_z = \left[ \left( \frac{\partial y}{\partial x} \right)_z \right]^{-1} , \quad \left( \frac{\partial x}{\partial y} \right)_z = \left( \frac{\partial x}{\partial w} \right)_z \left( \frac{\partial w}{\partial y} \right)_z , \quad \left( \frac{\partial x}{\partial y} \right)_z \left( \frac{\partial y}{\partial z} \right)_x \left( \frac{\partial z}{\partial x} \right)_y = -1$$

$$S = -k_B \sum_i p_i \ln p_i , \quad p_i = \frac{1}{Z} e^{-\beta E_i} , \quad Z = \sum_i e^{-\beta E_i} , \quad \beta \equiv \frac{1}{k_B T}$$

$$\Omega(T, V, \mu) = -k_B T \ln Z , \quad p_i = \frac{1}{Z} e^{-\beta(E_i - \mu N_i)} , \quad Z = \sum_i e^{-\beta(E_i - \mu N_i)}$$

$$\lambda_T = \left( \frac{2\pi\hbar^2}{mk_B T} \right)^{1/2} , \quad Z_1(T, V) = V \lambda_T^{-3} , \quad Z_N(T, V) = \frac{1}{N!} [Z_1(T, V)]^N$$

$$PV = Nk_B T = nRT , \quad U = \frac{3}{2} Nk_B T , \quad \left( \frac{dP}{dT} \right)_{\text{ex}} = \frac{\Delta S}{\Delta V} = \frac{L_{1 \rightarrow 2}}{T \Delta V_{1 \rightarrow 2}}$$

$$\langle n_i \rangle_{\text{FD}} = \frac{1}{e^{\beta(\epsilon_i - \mu)} + 1} T \xrightarrow{\theta(\epsilon_F - \epsilon_i)} 0 , \quad \frac{\partial \langle n_i \rangle_{\text{FD}}}{\partial \epsilon_i} T \xrightarrow{\theta(\epsilon_i - \epsilon_F)} 0 , \quad \langle n_i \rangle_{\text{BE}} = \frac{1}{e^{\beta(\epsilon_i - \mu)} - 1} , \quad \langle n_i \rangle_{\text{MB}} = e^{-\beta(\epsilon_i - \mu)}$$

$$\Omega_{\text{FD}} = -k_B T \sum_i \ln[1 + e^{-\beta(\epsilon_i - \mu)}] T \xrightarrow{\theta(\mu - \epsilon_i)} 0 - \sum_i (\mu - \epsilon_i) \theta(\mu - \epsilon_i) , \quad \Omega_{\text{BE}} = k_B T \sum_i \ln[1 - e^{-\beta(\epsilon_i - \mu)}]$$

$$\sum_i f(k_i) \approx \frac{gV}{2\pi^2} \int_0^\infty dk k^2 f(k) , \quad \epsilon(k) = \frac{\hbar^2 k^2}{2m} (NR) , \quad \epsilon(k) = \hbar ck (UR)$$

$$u(\omega, T) = \frac{\hbar}{\pi^2 c^3} \frac{\omega^3}{e^{\beta \hbar \omega} - 1} , \quad u(T) = a T^4 , \quad I(T) = \sigma T^4 , \quad a = \frac{\pi^2 k_B^4}{15 \hbar^3 c^3} , \quad \sigma = \frac{ac}{4}$$

$$\int_0^\infty dx \frac{x^p}{e^x - 1} = p! \zeta(p+1) , \quad \int_0^\infty dx \frac{x^p}{e^x + 1} = (1 - 2^{-p}) \zeta(p+1)$$

$$\zeta(s) = \sum_{n=1}^\infty \frac{1}{n^s} , \quad \zeta\left(\frac{3}{2}\right) \approx 2.61 , \quad \zeta(2) = \frac{\pi^2}{6} , \quad \zeta\left(\frac{5}{2}\right) \approx 1.34 , \quad \zeta(3) \approx 1.20 , \quad \zeta\left(\frac{7}{2}\right) \approx 1.13 , \quad \zeta(4) = \frac{\pi^4}{90}$$

$$\Gamma(p+1) = p! , \quad \Gamma(z+1) = z\Gamma(z) , \quad \Gamma\left(\frac{1}{2}\right) = \sqrt{\pi}$$

$$\int_0^\infty dx e^{-ax^2} = \frac{1}{2} \sqrt{\frac{\pi}{a}} , \quad \int_0^\infty dx x^{2n} e^{-ax^2} = (-1)^n \left[ \frac{d^n}{da^n} \frac{1}{2} \sqrt{\frac{\pi}{a}} \right]_{a=1}$$

$$\int_0^\infty dx x e^{-ax^2} = \frac{1}{2a} , \quad \int_0^\infty dx x^{2n+1} e^{-ax^2} = (-1)^n \left[ \frac{d^n}{da^n} \frac{1}{2a} \right]_{a=1}$$

$$\int d\epsilon \frac{f(\epsilon)}{e^{\beta(\epsilon - \mu)} + 1} \approx \int_0^\mu d\epsilon f(\epsilon) + \frac{\pi^2}{6} (k_B T)^2 \frac{df(\epsilon)}{d\epsilon} \Big|_\mu + \mathcal{O}(T^4)$$

$$\sum_{n=0}^\infty a x^n = \frac{a}{1-x} , \quad |x| < 1 , \quad \sum_{n=1}^\infty \frac{x^n}{n} = -\ln(1-x) , \quad |x| < 1 , \quad e^x = \sum_{n=0}^\infty \frac{x^n}{n!} , \quad (a+b)^n = \sum_{k=0}^n \binom{n}{k} a^k b^{n-k}$$

$$\frac{\partial f}{\partial t} + \dot{\mathbf{r}} \cdot \nabla f + \dot{\mathbf{p}} \cdot \nabla_{\mathbf{p}} f = -\frac{1}{\tau} (f - f_0) , \quad \dot{\mathbf{r}} = \mathbf{v} , \quad \dot{\mathbf{p}} = \mathbf{F}$$

$$\text{If } \frac{\partial f}{\partial t} = 0 \text{ and } f = f_0 + f' \text{ and } f' \ll f_0, \text{ then } f' \approx -\tau(\dot{\mathbf{r}} \cdot \nabla f_0 + \dot{\mathbf{p}} \cdot \nabla_{\mathbf{p}} f_0)$$