#### TIEA311 Tietokonegrafiikan perusteet kevät 2019

("Principles of Computer Graphics" – Spring 2019)

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Adapted from: *Wojciech Matusik*, and *Frédo Durand*: 6.837 Computer Graphics. Fall 2012. Massachusetts Institute of Technology: MIT OpenCourseWare, https://ocw.mit.edu/.

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Frontpage of the local course version, held during Spring 2019 at the Faculty of Information technology, University of Jyväskylä: http://users.jyu.fi/~nieminen/tgp19/

#### TIEA311 - Additional material

We did not have time to view this on lectures.

The following slides are the MIT course coverage on rasterization and modern GPU rendering.

Our follow-up course "TIES471 Real time rendering" probably starts with this topic, but if you decide to take the course later, you may be interested in looking at the material gathered here.

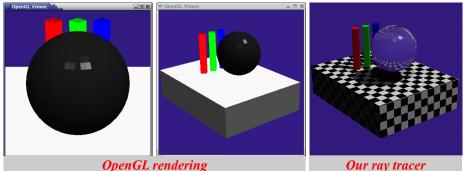
#### **Graphics Pipeline & Rasterization**

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# How Do We Render Interactively?

Use graphics hardware, via OpenGL or DirectX

 OpenGL is multi-platform, DirectX is MS only

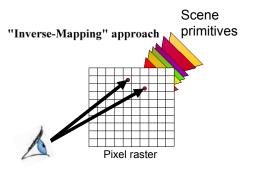


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• Most global effects available in ray tracing will be sacrificed for speed, but some can be approximated

# Ray Casting vs. GPUs for Triangles

Ray Casting For each pixel (ray) For each triangle Does ray hit triangle? Keep closest hit



# Ray Casting vs. GPUs for Triangles

Ray Casting

For each pixel (ray)

For each triangle

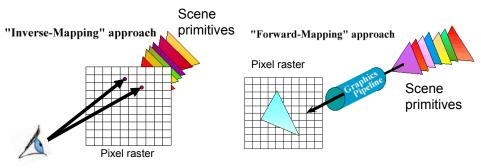
Does ray hit triangle? Keep closest hit

#### GPU

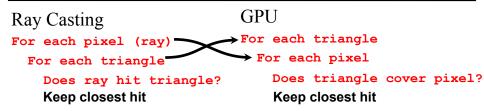
For each triangle

For each pixel

Does triangle cover pixel? Keep closest hit



# Ray Casting vs. GPUs for Triangles





# **GPUs do Rasterization**

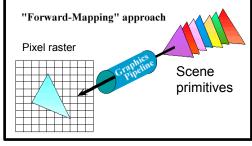
• The process of taking a triangle and figuring out which pixels it covers is called **rasterization** 

#### GPU

For each triangle

For each pixel

Does triangle cover pixel? Keep closest hit



# **GPUs do Rasterization**

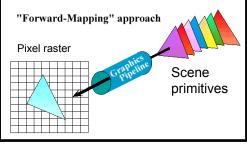
- The process of taking a triangle and figuring out which pixels it covers is called **rasterization**
- We've seen acceleration structures for ray tracing; rasterization is not stupid either
  - We're not actually going to test *all* pixels for each triangle

#### GPU

For each triangle

For each pixel

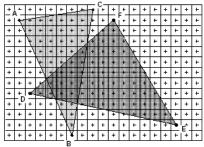
Does triangle cover pixel? Keep closest hit



# Rasterization ("Scan Conversion")

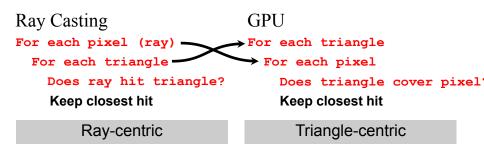
- Given a triangle's vertices & extra info for shading, figure out which pixels to "turn on" to render the primitive
- Compute illumination values to "fill in" the pixels within the primitive
- At each pixel, keep track of the closest primitive (z-buffer)
  - Only overwrite if triangle being drawn is closer than the previous triangle in that pixel

glBegin(GL\_TRIANGLES)
glNormal3f(...)
glVertex3f(...)
glVertex3f(...)
glVertex3f(...)
glLent();



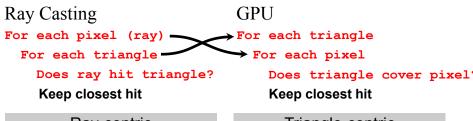
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### What are the Main Differences?



• What needs to be stored in memory in each case?

## What are the Main Differences?



Ray-centric

Triangle-centric

• In this basic form, ray tracing needs the entire scene description in memory at once

- Then, can sample the image completely freely

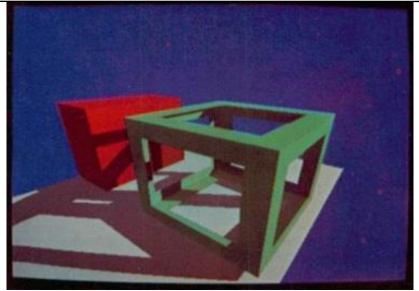
• The rasterizer only needs one triangle at a time, *plus* the entire image and associated depth information for all pixels

# **Rasterization Advantages**

- Modern scenes are more complicated than images
  - A 1920x1080 frame at 64-bit color and 32-bit depth per pixel is 24MB (not that much)
    - Of course, if we have more than one sample per pixel this gets larger, but e.g. 4x supersampling is still a relatively comfortable ~100MB
  - Our scenes are routinely larger than this
    - This wasn't always true

#### **Rasterization Advantages**

Weiler, Atherton 1977



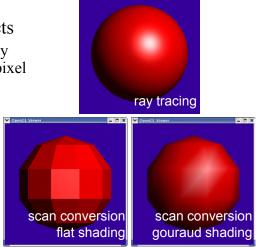
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# **Rasterization Advantages**

- Modern scenes are more complicated than images
  - A 1920x1080 frame (1080p) at 64-bit color and 32-bit depth per pixel is 24MB (not that much)
    - Of course, if we have more than one sample per pixel (later) this gets larger, but e.g. 4x supersampling is still a relatively comfortable ~100MB
  - Our scenes are routinely larger than this
    - This wasn't always true
- A rasterization-based renderer can *stream* over the triangles, no need to keep entire dataset around
  - Allows parallelism and optimization of memory systems

# **Rasterization Limitations**

- Restricted to scan-convertible primitives
  - Pretty much: triangles
- Faceting, shading artifacts
  - This is largely going away with programmable per-pixel shading, though
- No unified handling of shadows, reflection, transparency
- Potential problem of overdraw (high depth complexity)
  - Each pixel touched many times



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# Ray Casting / Tracing

- Advantages
  - Generality: can render anything that can be intersected with a ray
  - Easily allows recursion (shadows, reflections, etc.)
- Disadvantages
  - Hard to implement in hardware (lacks computation coherence, must fit entire scene in memory, bad memory behavior)
    - Not such a big point any more given general purpose GPUs
  - Has traditionally been too slow for interactive applications
  - Both of the above are changing rather rapidly right now!

- Input
  - Geometric model
    - · Triangle vertices, vertex normals, texture coordinates
  - Lighting/material model (shader)
    - Light source positions, colors, intensities, etc.
    - Texture maps, specular/diffuse coefficients, etc.
  - Viewpoint + projection plane
- Output
  - Color (+depth) per pixel

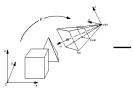
Colbert & Krivanek

Image of Real-Time Rendering of the Stanford Bunny with 40 Samples per Pixel removed due to copyright restrictions -- please see Fig. 20-1 from http://http. developer.nvidia.com/GPUGems3/gpugems3\_ch20.html for further details.

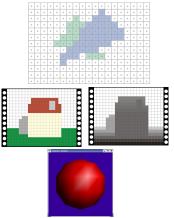


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- Project vertices to 2D (image)
- Rasterize triangle: find which pixels should be lit
- Test visibility (Z-buffer), update frame buffer color
- Compute per-pixel color

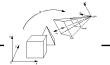


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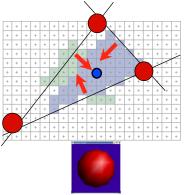


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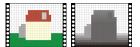
- Project vertices to 2D (image)
- Rasterize triangle: find which pixels should be lit
  - For each pixel, test 3 edge equations
    - if all pass, draw pixel
- Compute per-pixel color
- Test visibility (Z-buffer), update frame buffer color



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20

- Perform projection of vertices
- Rasterize triangle: find which pixels should be lit
- Compute per-pixel color
- Test visibility, update frame buffer color
  - Store minimum distance to camera © Khronos Group. All rights reserved. This content is for each pixel in "Z-buffer"
    - $\sim$ same as  $t_{min}$  in ray casting!
  - **if** newz < zbuffer[x,y]*zbuffer[x,y]=new z* framebuffer[x,y]=new color

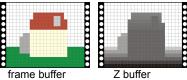
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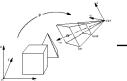
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For each triangle transform into eye space (perform projection) setup 3 edge equations for each pixel x,y if passes all edge equations compute z if z < zbuffer[x,y]zbuffer[x,y]=z framebuffer[x,y]=shade()

# **Questions?**

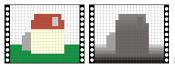


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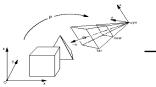


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# Projection

- Project vertices to 2D (image)
- Rasterize triangle: find which pixels should be lit
- Compute per-pixel color
- Test visibility (Z-buffer), update frame buffer

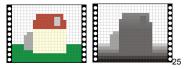


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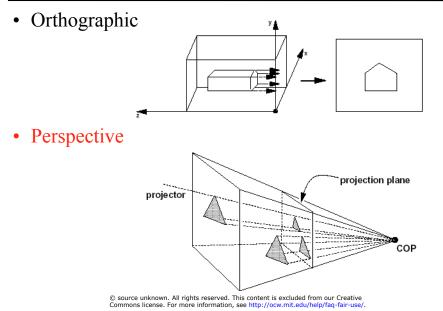


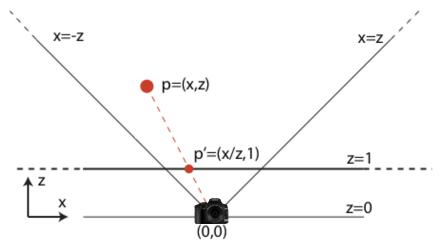


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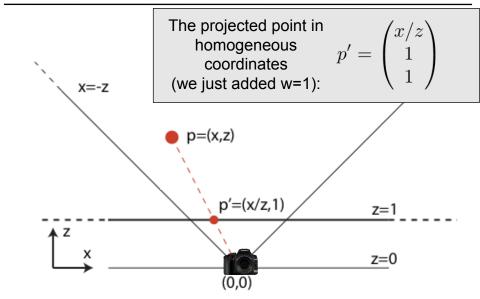


# Orthographic vs. Perspective

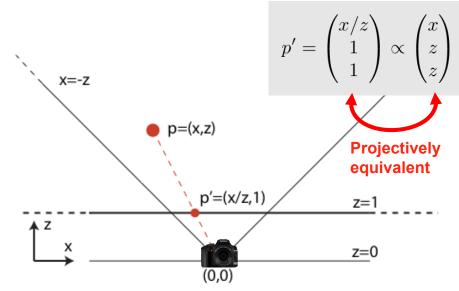




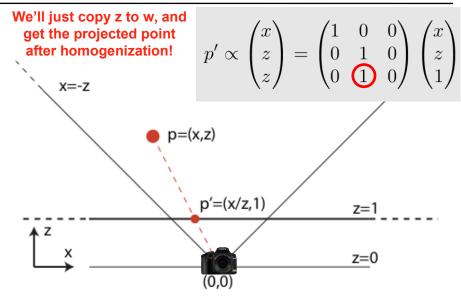
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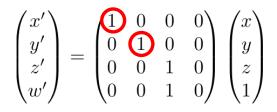
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## Extension to 3D

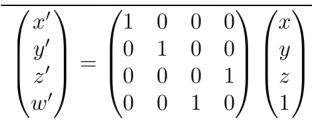
- Trivial: Just ass another dimension *y* and treat it like *x*
- Different fields of view and non-square image aspect ratios can be accomplished by simple scaling of the *x* and *y* axes.



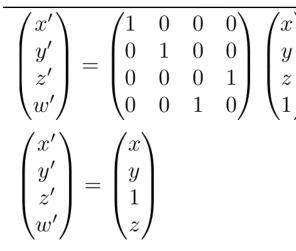
### Caveat

- These projections matrices work perfectly in the sense that you get the proper 2D projections of 3D points.
- However, since we are flattening the scene onto the z=1 plane, we've lost all information about the distance to camera.
  - We need the distance for Z buffering, i.e., figuring out what is in front of what!

#### Basic Idea: store 1/z



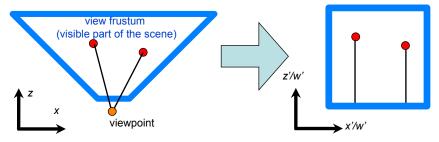
### Basic Idea: store 1/z



- z' = 1 before homogenization
- z'=1/z after homogenization

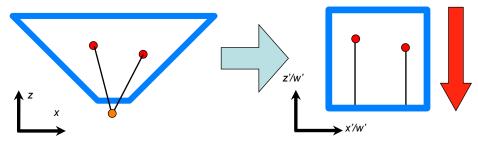
# Full Idea: Remap the View Frustum

• We can transform the frustum by a modified projection in a way that makes it a square (cube in 3D) after division by *w*'.



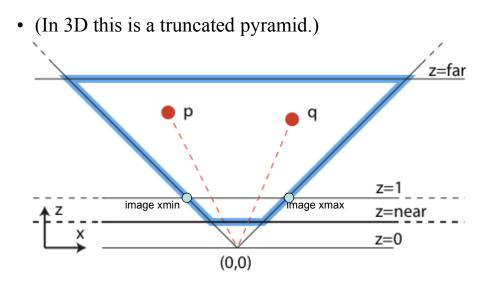
# The View Frustum in 2D

We can transform the frustum by a modified projection in a way that makes it a square (cube in 3D) after division by w'.



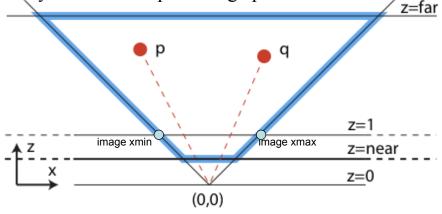
The final image is obtained by merely dropping the z coordinate after projection (orthogonal projection)

# The View Frustum in 2D

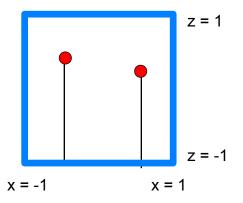


## The View Frustum in 2D

- Far and near are kind of arbitrary
- They bound the depth storage precision



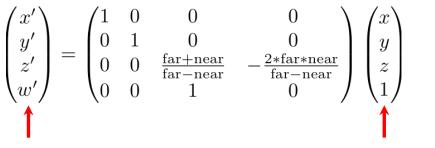
### The Canonical View Volume



 Point of the exercise: This gives screen coordinates and depth values for Z-buffering with unified math

 Caveat: OpenGL and DirectX define Z differently [0,1] vs.[-1,1]

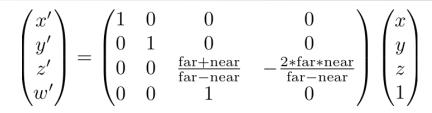
### OpenGL Form of the Projection



Homogeneous coordinates within canonical view volume

Input point in view coordinates

### OpenGL Form of the Projection



• 
$$z'=(az+b)/z=a+b/z$$

- where a & b depend on near & far

• Similar enough to our basic idea:

$$\begin{array}{c} -\mathbf{z}'=1/\mathbf{z} \\ & \begin{pmatrix} x' \\ y' \\ z' \\ w' \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix}$$

# Recap: Projection **Questions?**

- Perform rotation/translation/other transforms to put viewpoint at origin and view direction along z axis

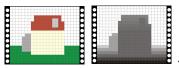
   This is the OpenGL "modelview" matrix
- Combine with projection matrix (perspective or orthographic)
  - Homogenization achieves foreshortening
  - This is the OpenGL "projection" matrix
- **Corollary**: The entire transform from object space to canonical view volume  $[-1,1]^3$  is a single matrix

# Modern Graphics Pipeline

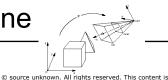
- Project vertices to 2D (image)
  - We now have screen coordinates
- Rasterize triangle: find which pixels should be lit
- Compute per-pixel color
- Test visibility (Z-buffer), update frame buffer

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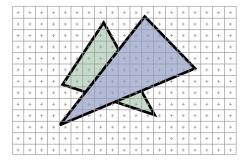






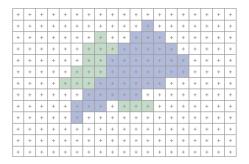
### 2D Scan Conversion

• Primitives are "continuous" geometric objects; screen is discrete (pixels)



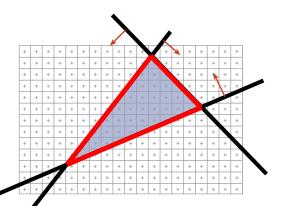
## 2D Scan Conversion

- Primitives are "continuous" geometric objects; screen is discrete (pixels)
- Rasterization computes a discrete approximation in terms of pixels (how?)



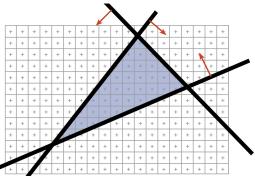
## **Edge Functions**

- The triangle's 3D edges project to line segments in the image (thanks to planar perspective)
  - Lines map to lines, not curves



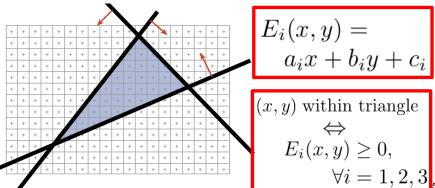
# **Edge Functions**

- The triangle's 3D edges project to line segments in the image (thanks to planar perspective)
- The interior of the triangle is the set of points that is inside all three halfspaces defined by these lines



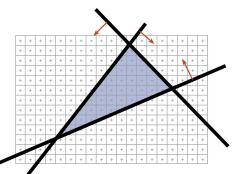
# **Edge Functions**

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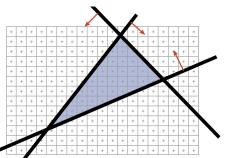
### **Brute Force Rasterizer**

- Compute E<sub>1</sub>, E<sub>2</sub>, E<sub>3</sub> coefficients from projected vertices
  - Called "triangle setup", yields  $a_i$ ,  $b_i$ ,  $c_i$  for i=1,2,3



### **Brute Force Rasterizer**

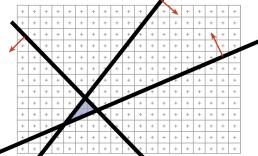
- Compute E<sub>1</sub>, E<sub>2</sub>, E<sub>3</sub> coefficients from projected vertices
- For each pixel (x, y)
  - Evaluate edge functions at pixel center
  - If all non-negative, pixel is in!



**Problem?** 

### **Brute Force Rasterizer**

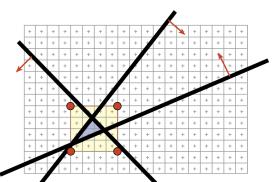
- Compute E<sub>1</sub>, E<sub>2</sub>, E<sub>3</sub> coefficients from projected vertices
- For each pixel (x, y)
  - Evaluate edge functions at pixel center
  - If all non-negative, pixel is in!



If the triangle is small, lots of useless computation if we really test all pixels

# **Easy Optimization**

- Improvement: Scan over only the pixels that overlap the *screen bounding box* of the triangle
- How do we get such a bounding box?
  - $X_{\text{min}}, X_{\text{max}}, Y_{\text{min}}, Y_{\text{max}}$  of the projected triangle vertices



### Rasterization Pseudocode

For every triangle

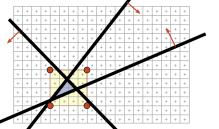
- Compute projection for vertices, compute the  $\ensuremath{\mathtt{E}}_{\ensuremath{\mathtt{i}}}$
- Compute bbox, clip bbox to screen limits

For all pixels in bbox

Evaluate edge functions  $E_i$ 

If all > 0

Framebuffer[x,y ] = triangleColor



Bounding box clipping is easy, just clamp the coordinates to the screen rectangle

Note: No

visibility



## **Incremental Edge Functions**

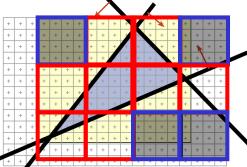
```
For every triangle
ComputeProjection
Compute bbox, clip bbox to screen limits
For all scanlines y in bbox
Evaluate all E<sub>i</sub>'s at (x0,y): E<sub>i</sub> = a<sub>i</sub>x0 + b<sub>i</sub>y + c<sub>i</sub>
For all pixels x in bbox
If all E<sub>i</sub>>0
Framebuffer[x,y] = triangleColor
Increment line equations: E<sub>i</sub> += a<sub>i</sub>
```

 We save ~two multiplications and two additions per pixel when the triangle is large

Can also zig-zag to avoid reinitialization per scanline, just initialize once at x0, y0

### Indeed, We Can Be Smarter

- Hierarchical rasterization!
  - Conservatively test blocks of pixels before going to per-pixel level (can skip large blocks at once)
  - Usually two levels



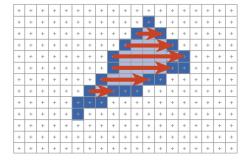
Can also test if an entire block is **inside** the triangle; then, can skip edge functions tests for all pixels for even further speedups.(Must still test Z, because they might still be occluded.)

### **Further References**

- Henry Fuchs, Jack Goldfeather, Jeff Hultquist, Susan Spach, John Austin, Frederick Brooks, Jr., John Eyles and John Poulton, "Fast Spheres, Shadows, Textures, Transparencies, and Image Enhancements in Pixel-Planes", Proceedings of SIGGRAPH '85 (San Francisco, CA, July 22–26, 1985). In *Computer Graphics*, v19n3 (July 1985), ACM SIGGRAPH, New York, NY, 1985.
- Juan Pineda, "A Parallel Algorithm for Polygon Rasterization", Proceedings of SIGGRAPH '88 (Atlanta, GA, August 1–5, 1988). In *Computer Graphics*, v22n4 (August 1988), ACM SIGGRAPH, New York, NY, 1988. Figure 7: Image from the spinning teapot performance test.
- Marc Olano Trey Greer, "Triangle Scan Conversion using 2D Homogeneous Coordinates", Graphics Hardware 97 http://www.cs.unc.edu/~olano/papers/2dh-tri/2dh-tri.pdf

## **Oldschool Rasterization**

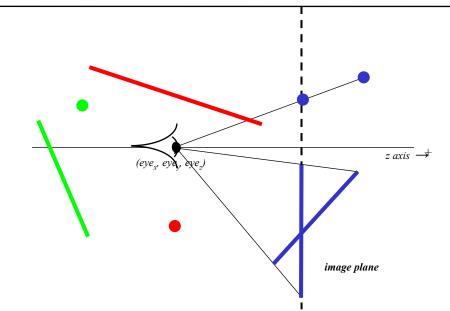
- Compute the boundary pixels using line rasterization
- Fill the spans



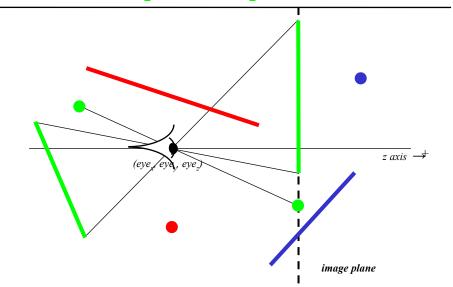
#### More annoying to implement than edge functions

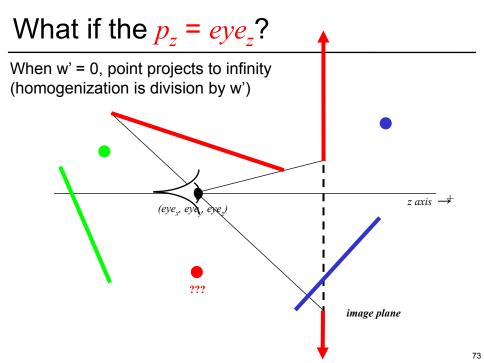
Not faster unless triangles are huge

What if the  $p_z$  is >  $eye_z$ ?



What if the  $p_z$  is  $< eye_z$ ?

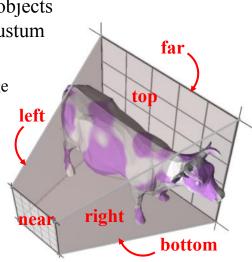




# A Solution: Clipping "clip" geometry to view frustum, discard outside parts z axis $\rightarrow$ (eye, eye, eye z=far z=near image plane

# Clipping

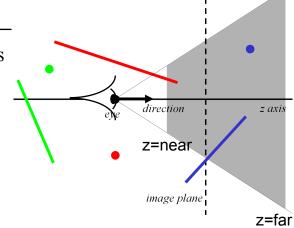
- Eliminate portions of objects outside the viewing frustum
- View Frustum
  - boundaries of the image plane projected in 3D
  - a near & far clipping plane
- User may define additional clipping planes



Leonard McMillan, Computer Science at the University of North Carolina in Chapel Hill.

# Why Clip?

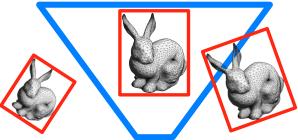
- Avoid degeneracies
  - Don't draw stuff behind the eye
  - Avoid division
     by 0 and overflow



**Questions?** 

- "View Frustum Culling"
  - Use bounding volumes/hierarchies to test whether any part of an object is within the view frustum
    - Need "frustum vs. bounding volume" intersection test
    - Crucial to do hierarchically when scene has lots of objects!
    - Early rejection (different from clipping)

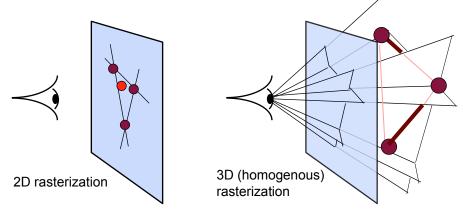
See e.g. Optimized view frustum culling algorithms for bounding boxes, Ulf Assarsson and Tomas Möller, journal of graphics tools, 2000.



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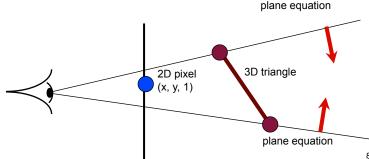
- Idea: avoid projection (and division by zero) by performing rasterization in 3D
  - Or equivalently, use 2D homogenous coordinates
     (w'=z after the projection matrix, remember)
- Motivation: clipping is annoying
- Marc Olano, Trey Greer: Triangle scan conversion using 2D homogeneous coordinates, Proc. ACM SIGGRAPH/Eurographics Workshop on Graphics Hardware 1997

- Replace 2D edge equation by 3D plane equation
  - Treat pixels as 3D points (x, y, 1) on image plane, test for containment in 3 halfspaces just like edge functions



Given 3D triangle

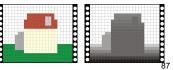
- setup plane equations
- (plane through viewpoint & triangle edge)
- For each pixel x,y
  - compute plane equations for (x,y,1)
  - if all pass, draw pixel



- Works for triangles behind eye
- Still linear, can evaluate incrementally/hierarchically like 2D 2D pixel (x', y', 1) 3D triangle

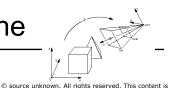
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- Rasterize triangle: find which pixels should be lit
- Compute per-pixel color
- Test visibility, update frame buffer
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# **Modern Graphics Pipeline**

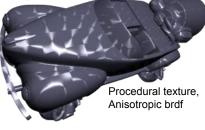
• Perform projection of vertices





## **Pixel Shaders**

- Modern graphics hardware enables the execution of rather complex programs to compute the color of every single pixel
- More later Translucence Backlighting

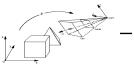




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# Modern Graphics Pipeline

- Perform projection of vertices
- Rasterize triangle: find which pixels should be lit
- Compute per-pixel color
- Test visibility, update frame buffer

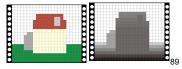


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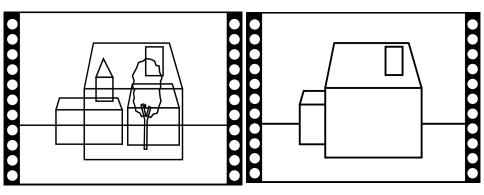


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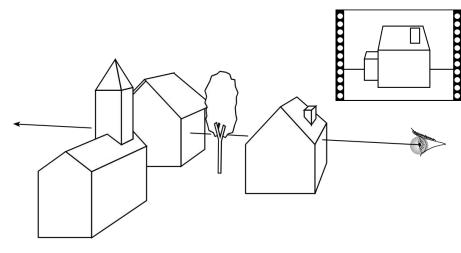
# Visibility

• How do we know which parts are visible/in front?



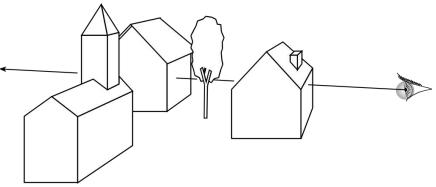
# **Ray Casting**

• Maintain intersection with closest object



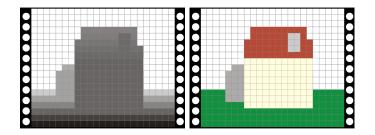
# Visibility

- In ray casting, use intersection with closest t
- Now we have swapped the loops (pixel, object)
- What do we do?



### Z buffer

- In addition to frame buffer (R, G, B)
- Store distance to camera (*z*-buffer)
- Pixel is updated only if *newz* is closer than *z*-buffer value



### Z-buffer pseudo code

For every triangle Compute Projection, color at vertices Setup line equations Compute bbox, clip bbox to screen limits For all pixels in bbox Increment line equations

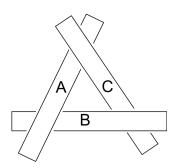
#### Compute curentZ

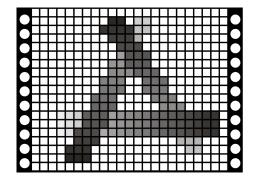
Compute currentColor

If all line equations>0 //pixel [x,y] in triangle

If currentZ<zBuffer[x,y] //pixel is visible
Framebuffer[x,y]=currentColor
zBuffer[x,y]=currentZ</pre>

### Works for hard cases!





### More questions for next time

- How do we get Z?
- Texture Mapping?

