

IDS

JYU

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Direct detection of light dark matter

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Outline

1. Introduction

2. Results

3. Conclusions

Based on `ArXiv:1903.08654` (to appear in PRD)

In collaboration with

Nader Mirabolfathi (Univ. Texas A & M)

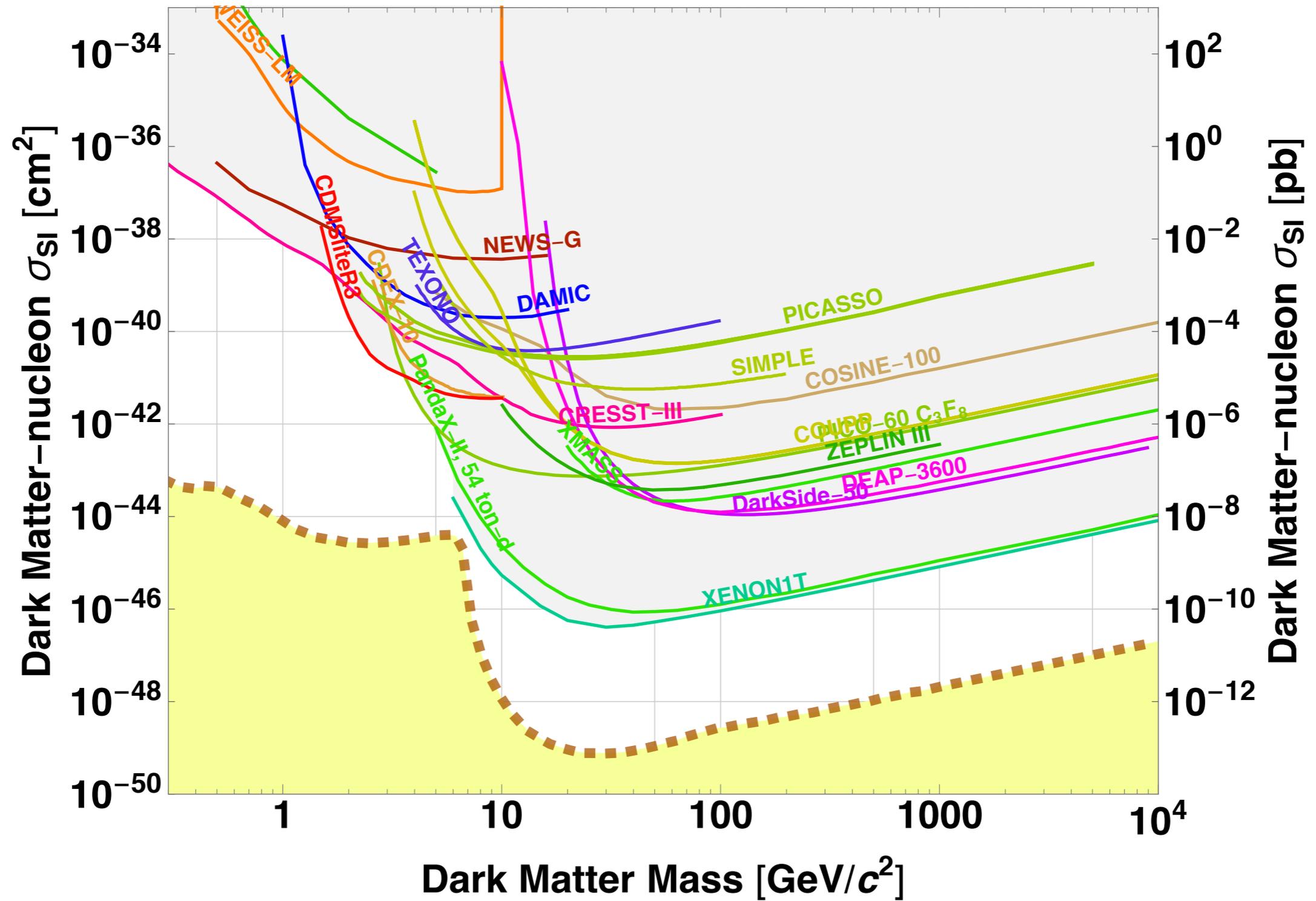
Kai Nordlund and Matti Heikinheimo (Univ. of Helsinki)

1. Introduction

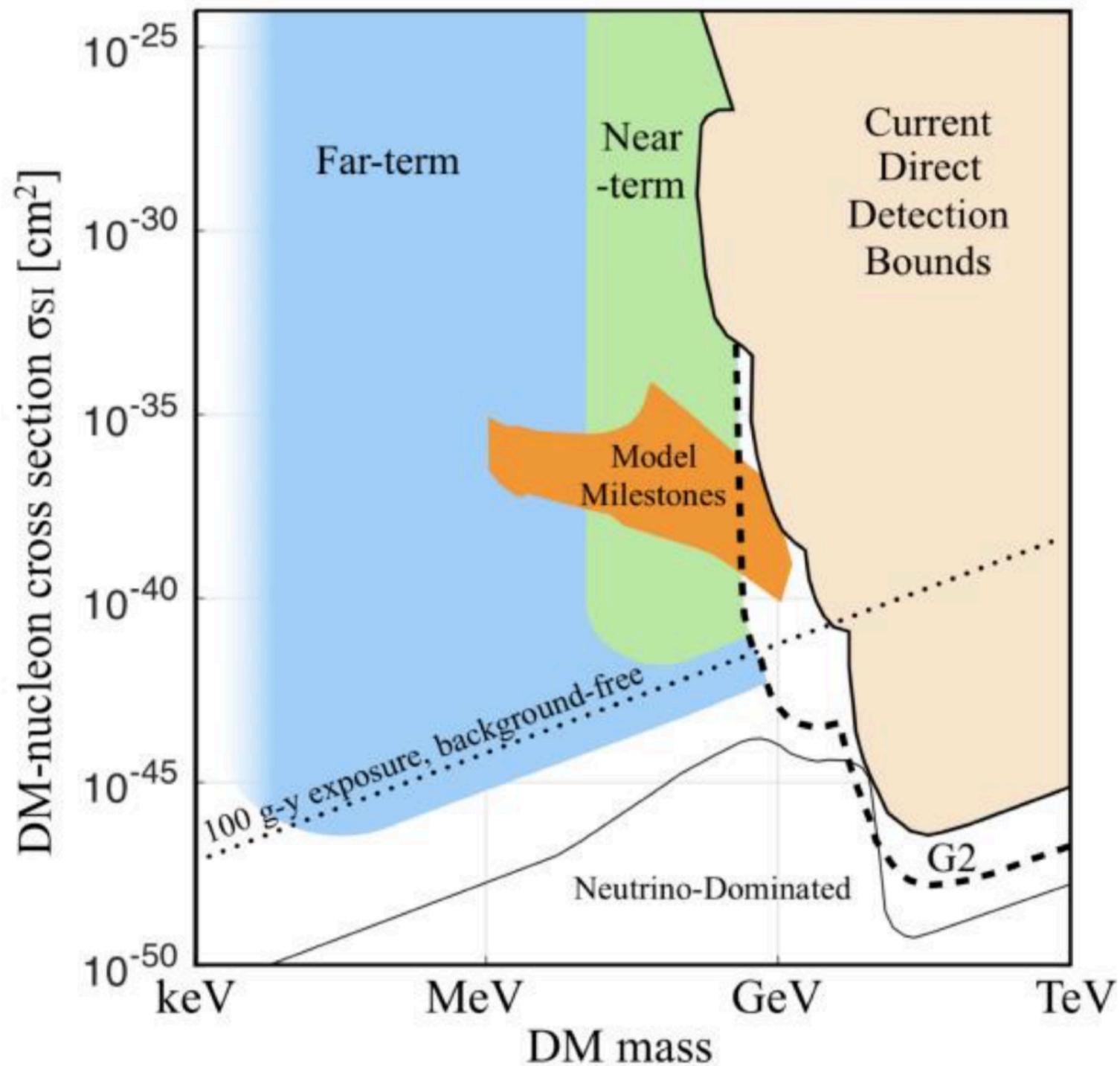
Dark Matter Mass Range



The present



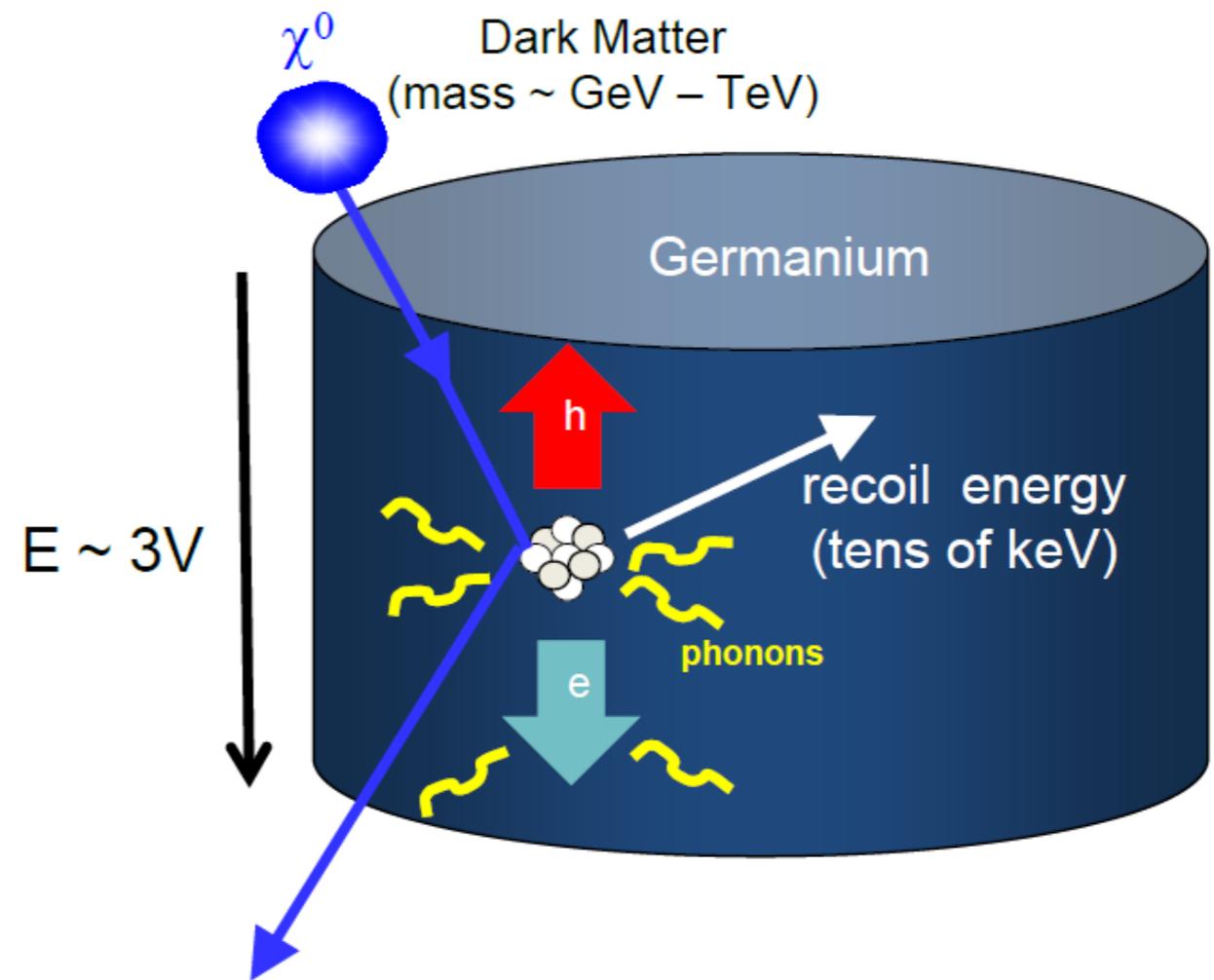
The future



Several new technologies/ detector concepts under active R&D, see

https://science.energy.gov/~media/hep/pdf/Reports/Dark_Matter_New_Initiatives_rpt.pdf

CDMS experiment:



Smaller DM masses, smaller recoils
Higher sensitivity needed.
Means: single electron resolution.

Development beyond G2, e.g. by Nader Mirabolfathi's group (Texas A&M)

Scattering in a solid: Radiation damage

Extensively studied for beams of ordinary matter.

A key quantity: threshold displacement energy T_d

Simple idea:

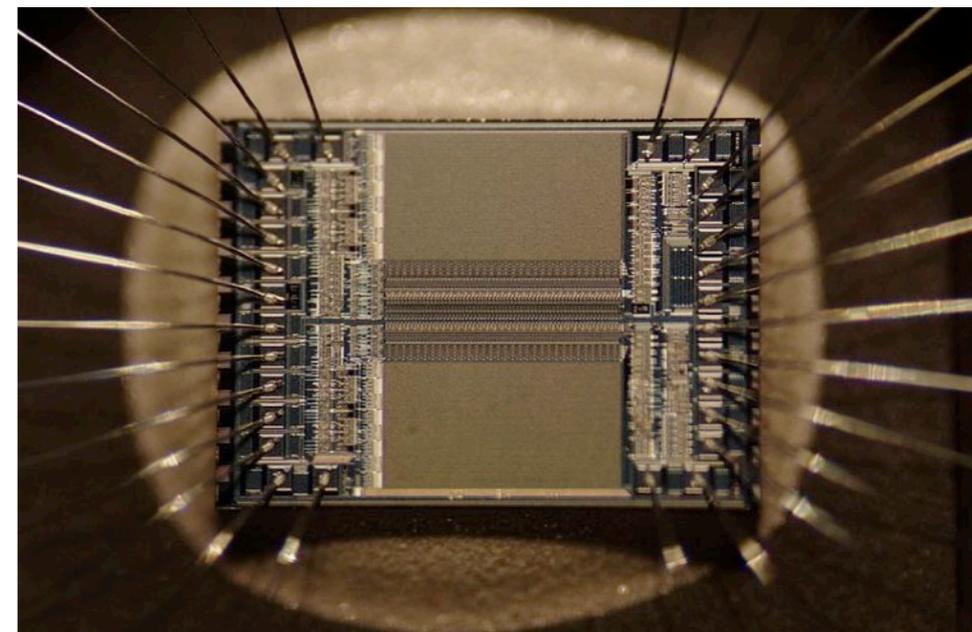
Minimum energy needed to displace an atom in a crystal.

Typical values for metals and semiconductors: $T_d \sim 20\dots 50 \text{ eV}$

Important in estimating damage production

Kinchin-Pease:
$$N_{\text{Frenckel}} \sim \frac{T}{2T_d}$$

e.g. in Si chip manufacturing.



Scattering in a solid: Radiation damage

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Consider DM scattering on nucleus:

$$m_{\text{DM}} = 1 \text{ GeV}$$

$$\Rightarrow E_{\text{DM}} = 269 \text{ eV}$$

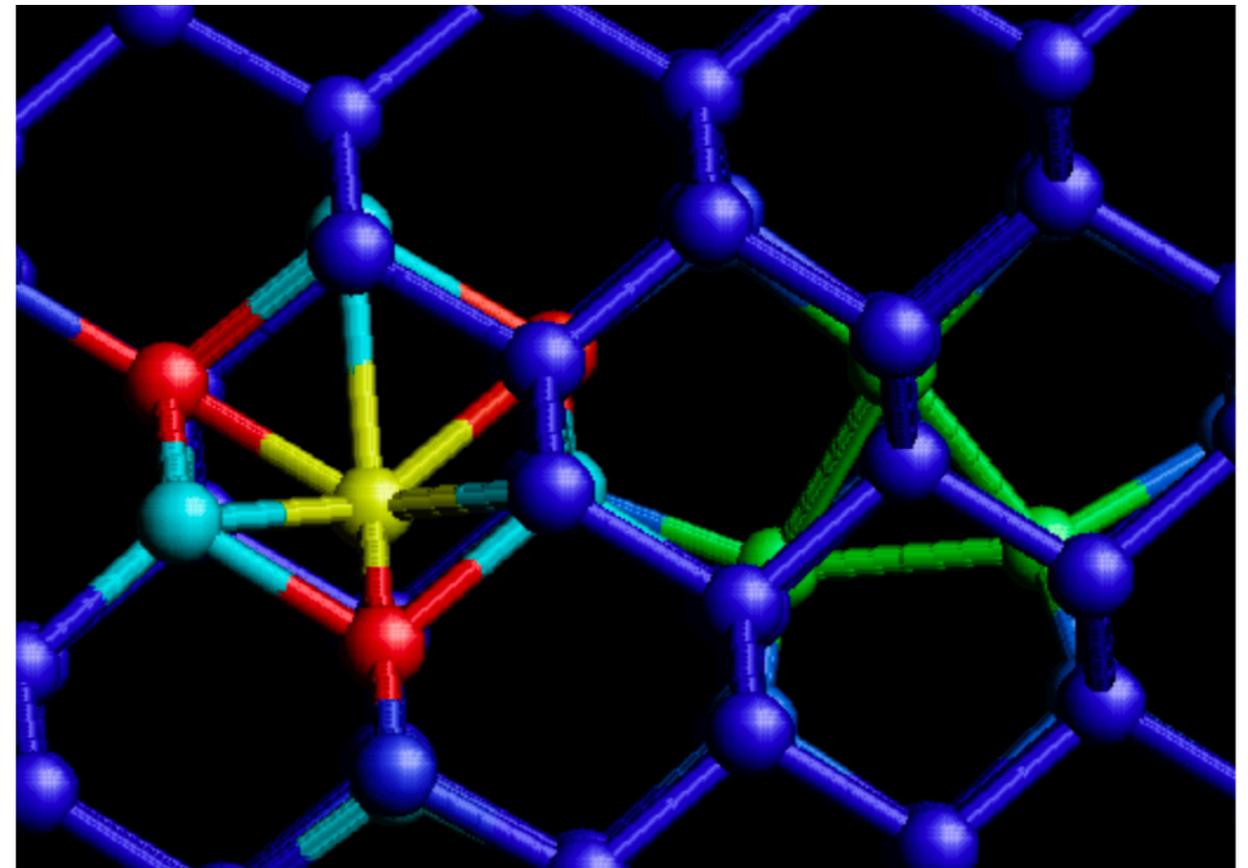
$$v_{\text{DM}} = 220 \text{ km/s}$$

Energy transfer to Silicon $M = 28 \text{ u}$ in head on collision:

$$T = \frac{4Mm_{\text{DM}}}{(M + m_{\text{DM}})^2} E_{\text{DM}} = 38 \text{ eV}$$

**Obviously, the threshold
must depend on crystal direction**

Experimentally verified
in electron irradiation experiments
(since '70s)



Computable by molecular dynamics simulations.

Molecular Dynamics

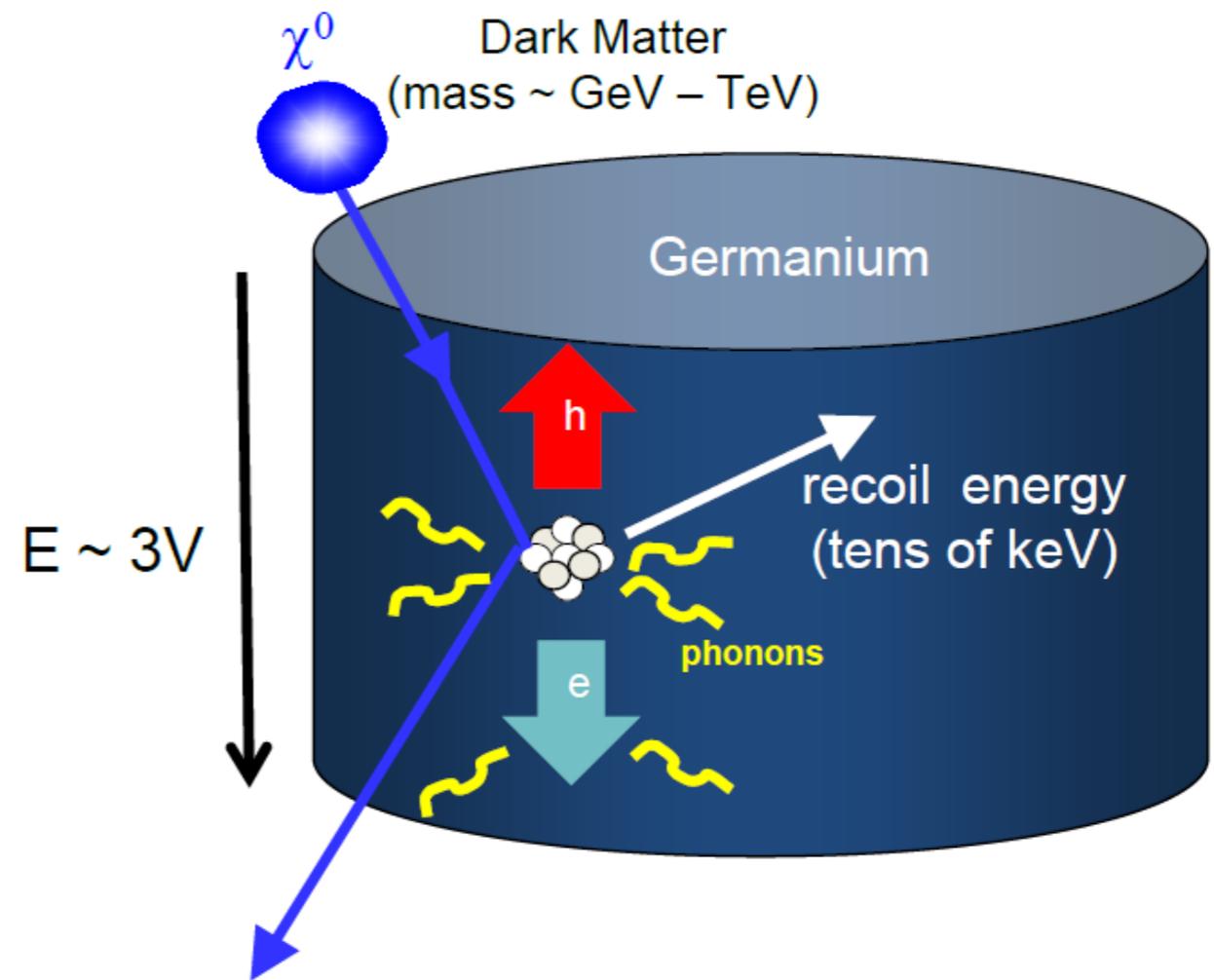
= simulation of atomic motion by solving Newton's equation.

Forces from quantum or classical modelling:

Quantum: density functional theory

Classical: analytic interatomic potentials

CDMS experiment:



Recoiling nucleus forms a lattice defect.

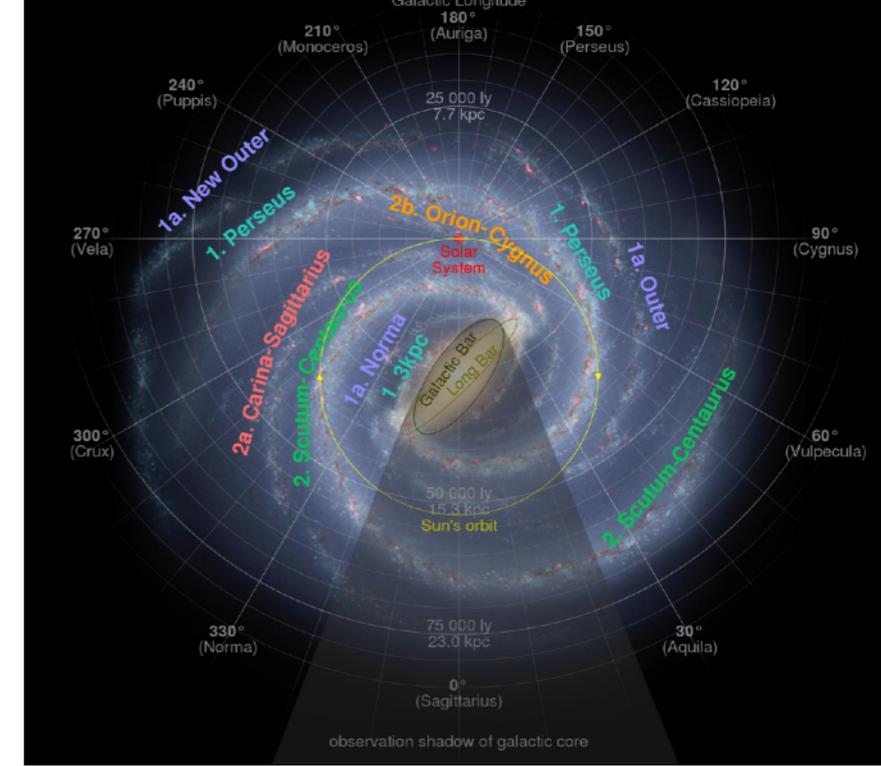
Facilitates e-h creation.

Directional sensitivity due to $T_d(\theta, \phi)$

Constant level of recoils as the Sun moves in the galaxy

Simple idea:

Detector moves with respect to the dark matter background.
Depending on this, the energy transfer can be above or below threshold.

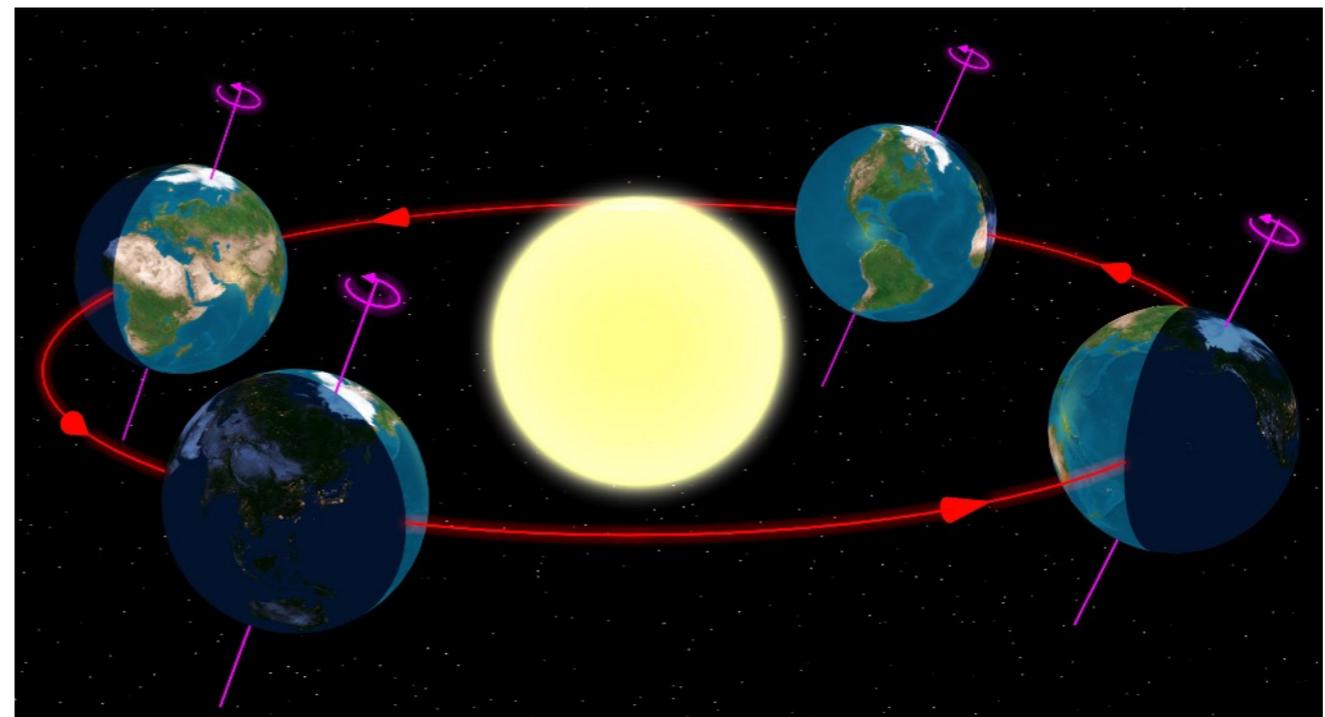


Additional effects from relative movement:

Annual modulation:
motion of Earth around Sun.

Daily modulation:
rotation of Earth.

Will distinguish the DM signal from BG



2. Detailed analysis

The event rate

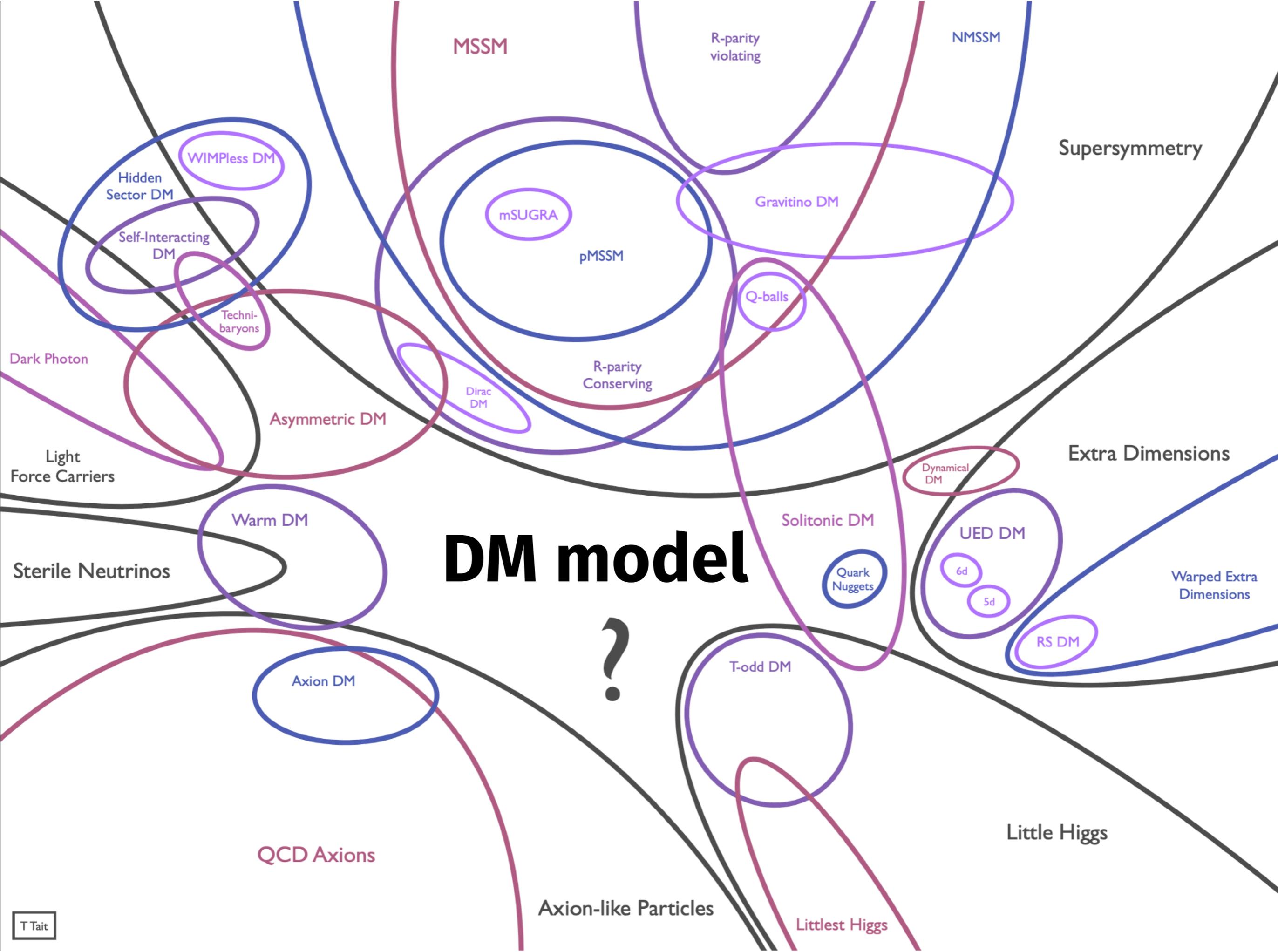
$$v_{\min} = \sqrt{\frac{m_N E}{2\mu^2}}$$

Kinematics

$$\frac{dR}{dE d\Omega_q} \sim \int d^3v \underbrace{|\mathcal{M}|^2}_{\text{DM model}} \underbrace{f_{\text{SHM}}(v)}_{\text{Standard Halo Model}} \overbrace{\delta(\mathbf{v} \cdot \hat{\mathbf{q}} - v_{\min})}^{\text{Kinematics}}$$

$$f_{\text{SHM}}(v) = \frac{1}{\mathcal{N}} \frac{1}{(2\pi\sigma_v^2)^{3/2}} \exp(-v^2/(2\sigma_v^2)) \Theta(v_e - v)$$

DM model



MSSM

R-parity violating

NMSSM

Supersymmetry

WIMPless DM

Hidden Sector DM

Self-Interacting DM

Techni-baryons

mSUGRA

pMSSM

Gravitino DM

Q-balls

R-parity Conserving

Dirac DM

Asymmetric DM

Dark Photon

Light Force Carriers

Extra Dimensions

Dynamical DM

Warm DM

Solitonic DM

UED DM

6d

5d

Warped Extra Dimensions

Sterile Neutrinos

Quark Nuggets

RS DM

DM model



T-odd DM

Axion DM

QCD Axions

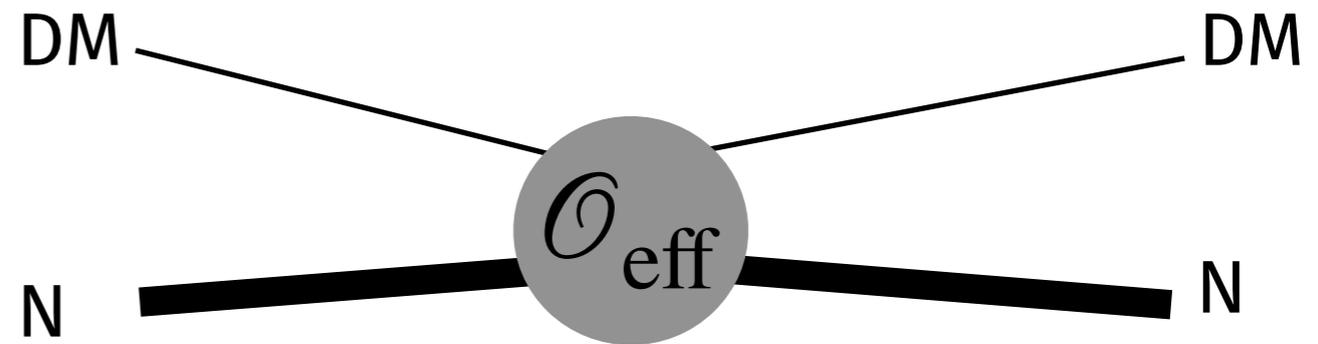
Little Higgs

Axion-like Particles

Littlest Higgs

DM effective theory

At low energy most models look like



Modest number of general eff. operators

Fitzpatrick, Haxton, Katz, Lubbers, Xu, JCAP (2013)
Anand, Fitzpatrick, Haxton, PRC (2014)

Eff. operators can depend only on

$$\mathbf{q}, \quad \mathbf{v}^\perp, \quad \mathbf{S}_{\text{DM}}, \quad \mathbf{S}_n$$

$$\mathbf{v}^\perp = \mathbf{v}_{\text{rel}} + \frac{\mathbf{q}}{2\mu_{\text{DM},n}}$$

$$\Rightarrow |\mathcal{M}|^2 = a_1 1 + a_2 q^2 + a_3 q^4 + b_1 v_\perp^2 + \dots$$

$$\begin{aligned}\mathcal{O}_1 &= 1 \\ \mathcal{O}_2 &= (v^\perp)^2 \\ \mathcal{O}_3 &= i\mathbf{S}_n \cdot \left(\frac{\mathbf{q}}{m_n} \times \mathbf{v}^\perp\right) \\ \mathcal{O}_4 &= \mathbf{S}_{\text{DM}} \cdot \mathbf{S}_n \\ \mathcal{O}_5 &= i\mathbf{S}_{\text{DM}} \cdot \left(\frac{\mathbf{q}}{m_n} \times \mathbf{v}^\perp\right) \\ \mathcal{O}_6 &= (\mathbf{S}_{\text{DM}} \cdot \mathbf{q})(\mathbf{S}_n \cdot \mathbf{q})\end{aligned}$$

$$\begin{aligned}\mathcal{O}_7 &= \mathbf{S}_n \cdot \mathbf{v}^\perp \\ \mathcal{O}_8 &= \mathbf{S}_{\text{DM}} \cdot \mathbf{v}^\perp \\ \mathcal{O}_9 &= i\mathbf{S}_{\text{DM}} \cdot (\mathbf{S}_n \times \mathbf{q}) \\ \mathcal{O}_{10} &= \mathbf{S}_n \cdot \mathbf{q} \\ \mathcal{O}_{11} &= \mathbf{S}_{\text{DM}} \cdot \mathbf{q} \\ \mathcal{O}_{12} &= i\mathbf{S}_{\text{DM}} \cdot (\mathbf{S}_n \times \mathbf{v}^\perp)\end{aligned}$$

$$\begin{aligned}\mathcal{O}_{13} &= i(\mathbf{S}_{\text{DM}} \cdot \mathbf{v}^\perp)(\mathbf{S}_n \cdot \frac{\mathbf{q}}{m_n}) \\ \mathcal{O}_{14} &= i(\mathbf{S}_{\text{DM}} \cdot \frac{\mathbf{q}}{m_n})(\mathbf{S}_n \cdot \mathbf{v}^\perp) \\ \mathcal{O}_{15} &= -(\mathbf{S}_{\text{DM}} \cdot \frac{\mathbf{q}}{m_n})((\mathbf{S}_n \times \mathbf{v}^\perp) \cdot \frac{\mathbf{q}}{m_n}) \\ \mathcal{O}_1^{LR} &= \frac{\mathcal{O}_1}{q^2}\end{aligned}$$

e.g. usual SI and SD:

$$\mathcal{O}_{\text{SI}} = \mathcal{O}_1$$

$$\mathcal{O}_{\text{SD}} = \mathcal{O}_4$$

but more general behaviors possible:

$$|\mathcal{M}|^2 \propto \begin{cases} 1 & : \mathcal{O}_1, \mathcal{O}_4, \\ v_\perp^2 & : \mathcal{O}_7, \mathcal{O}_8, \\ q^2 & : \mathcal{O}_9, \mathcal{O}_{10}, \mathcal{O}_{11}, \mathcal{O}_{12} \\ v_\perp^2 q^2 & : \mathcal{O}_5, \mathcal{O}_{13}, \mathcal{O}_{14}, \\ q^4 & : \mathcal{O}_3, \mathcal{O}_6, \\ q^4 (q^2 + v_\perp^2) & : \mathcal{O}_{15}, \\ q^{-4} & : \mathcal{O}_1^{LR}. \end{cases}$$

We consider: $|\mathcal{M}|^2 = a_1 1 + a_2 q^2 + a_3 q^4 + b_1 v_\perp^2 + \dots$

Two integrals over velocity distribution

The Radon transform:

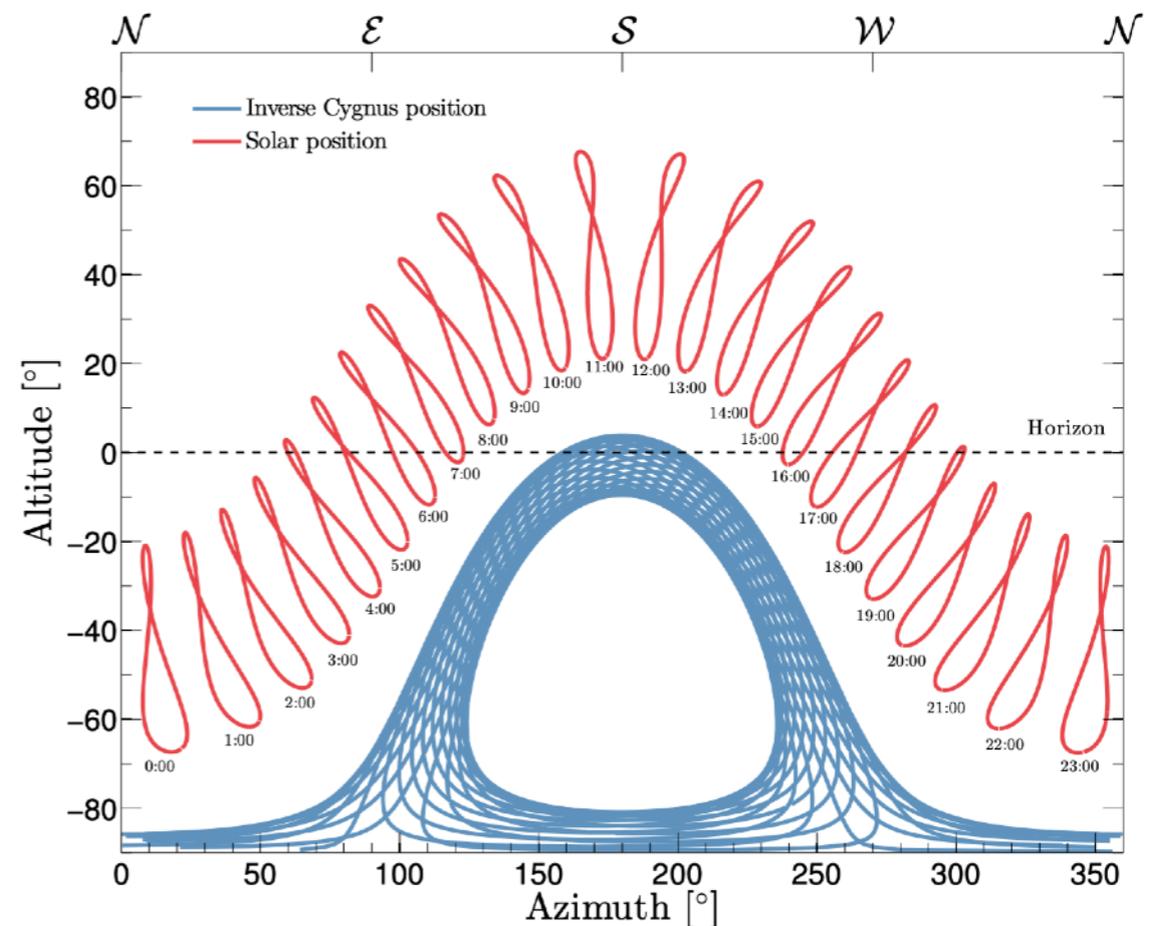
$$\hat{f}(v_{\min}, \hat{\mathbf{q}}) = \int \delta(\mathbf{v} \cdot \hat{\mathbf{q}} - v_{\min}) f(\mathbf{v}) d^3v$$

The transverse Radon transform:

$$\hat{f}_T(v_{\min}, \hat{\mathbf{q}}) = \int \delta(\mathbf{v} \cdot \hat{\mathbf{q}} - v_{\min}) (v^\perp)^2 f(\mathbf{v}) d^3v$$

From galactic rest frame to the lab-frame: $\mathbf{v} \rightarrow \mathbf{v} - \mathbf{V}(\mathbf{t})$

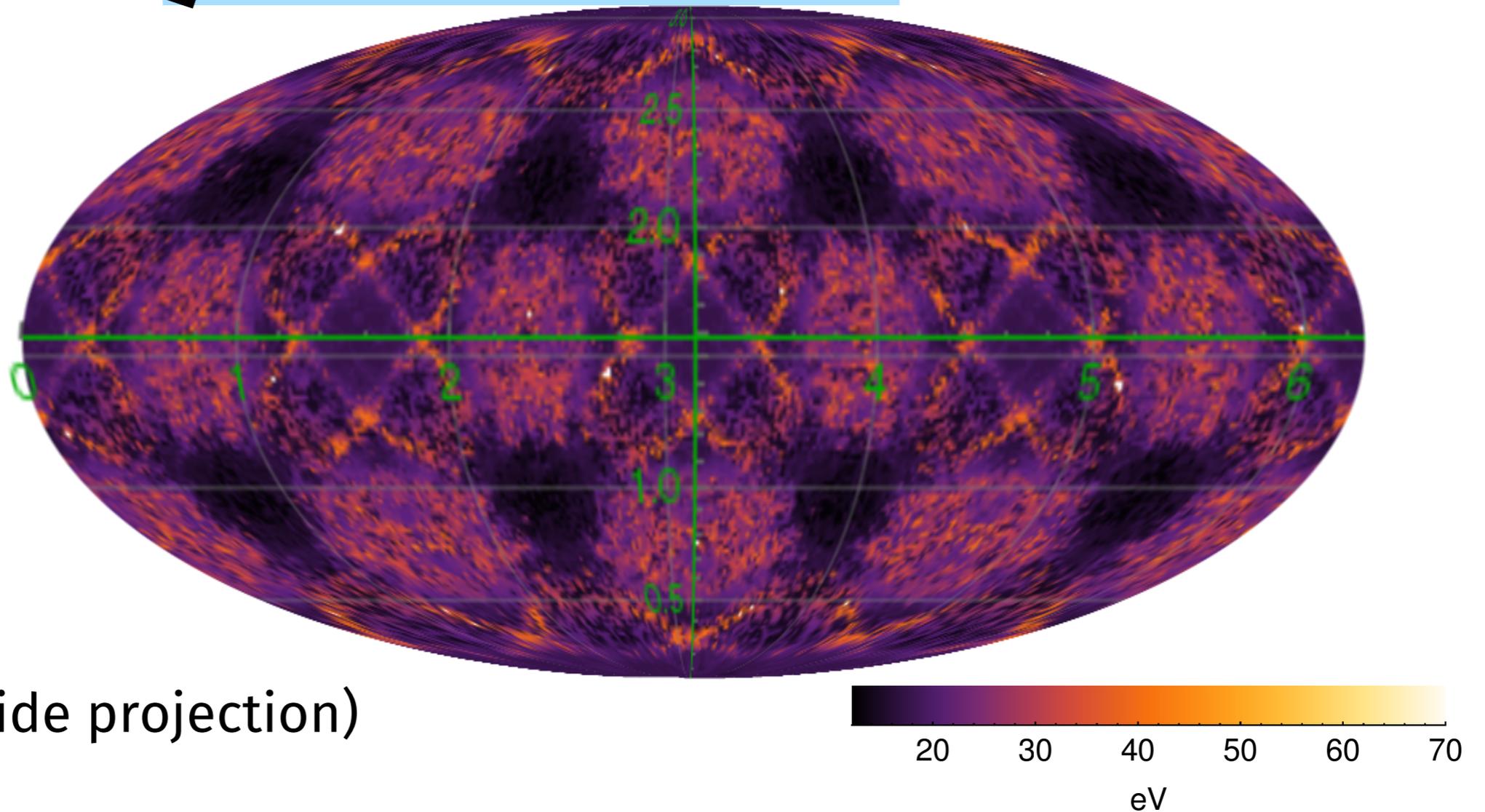
C.A.J. O'Hare *et al.*
1505.08061



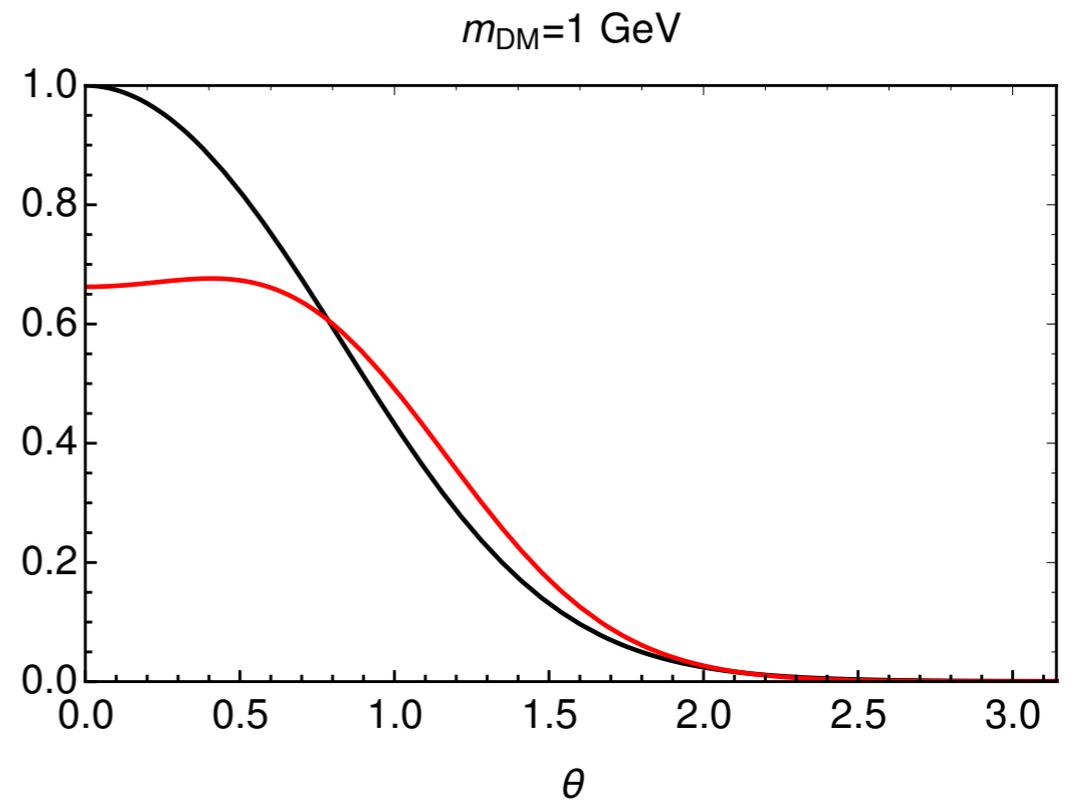
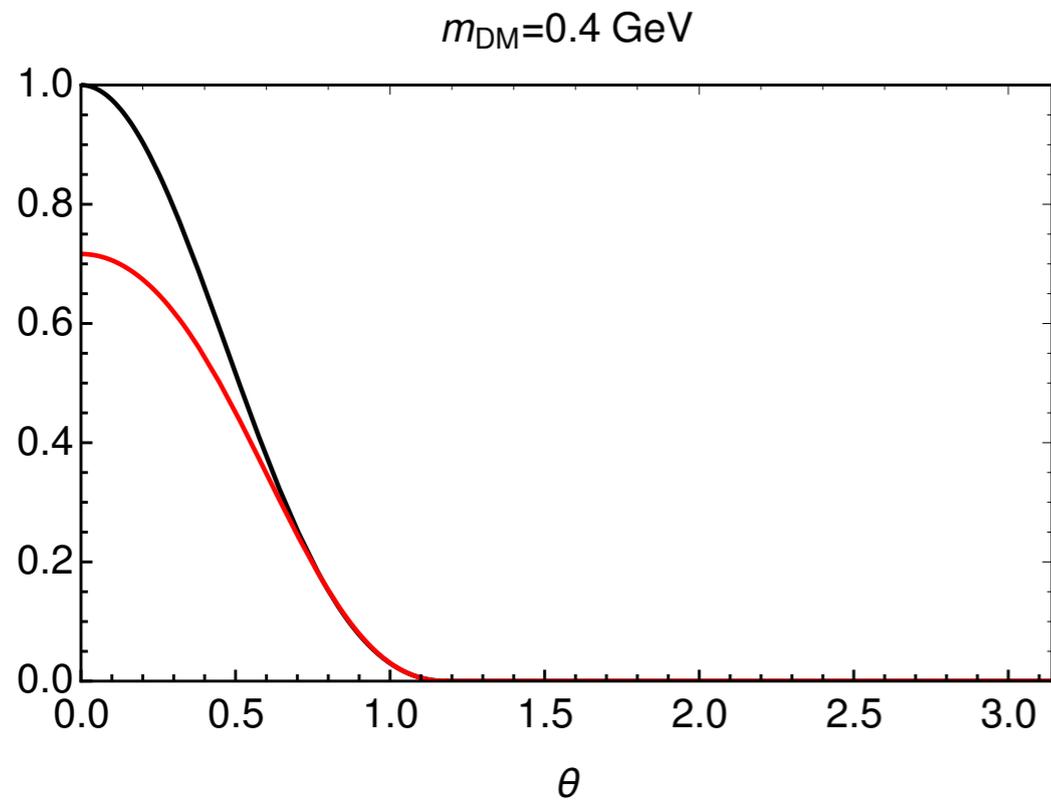
$$|\mathcal{M}|^2 = a_1 1 + a_2 q^2 + a_3 q^4 + b_1 v_{\perp}^2 + \dots$$

$$\frac{dR}{d\Omega_q} \sim \int_{E_{\min}(\theta, \phi)}^{E_{\max} \approx \infty} \left[(a_1 + a_2 q^2 + \dots) \hat{f}(v_{\min}, \hat{\mathbf{q}}) + (b_1 + \dots) \hat{f}_T(v_{\min}, \hat{\mathbf{q}}) \right]$$

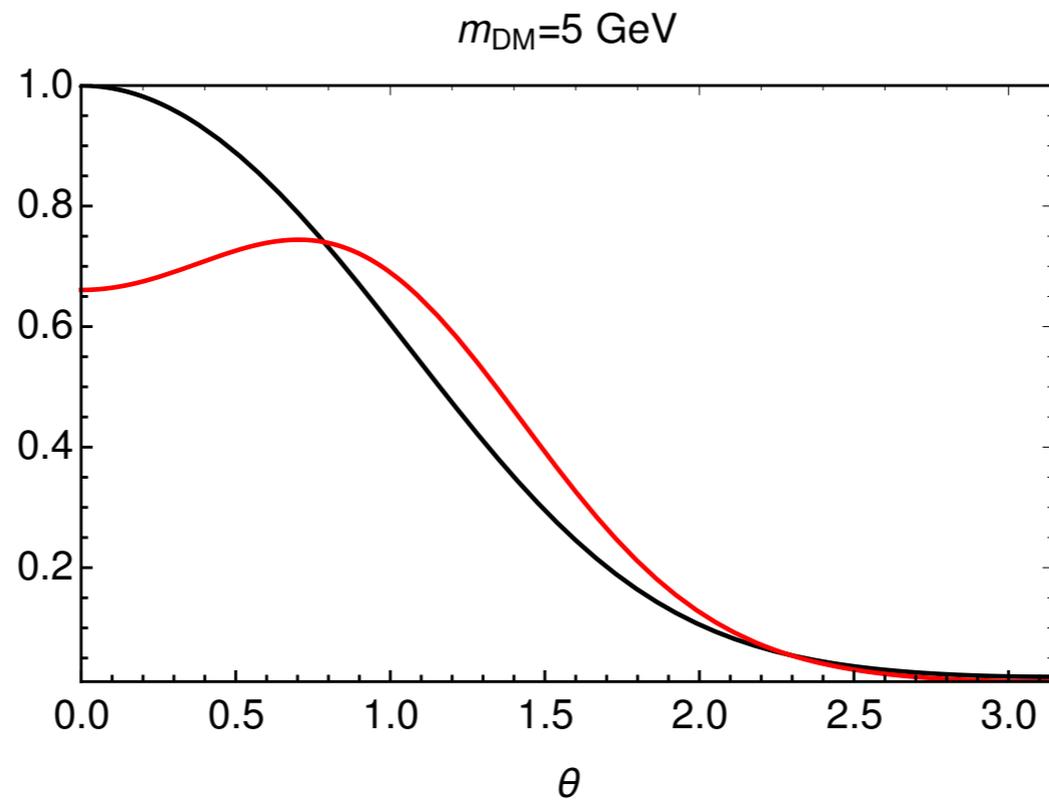
Threshold energies for Ge



Radon vs. **transverse Radon** trafo:



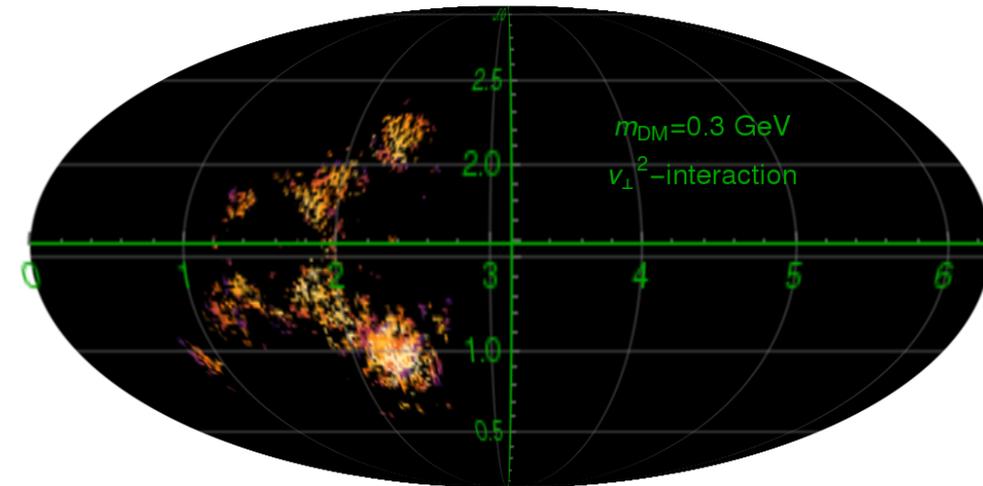
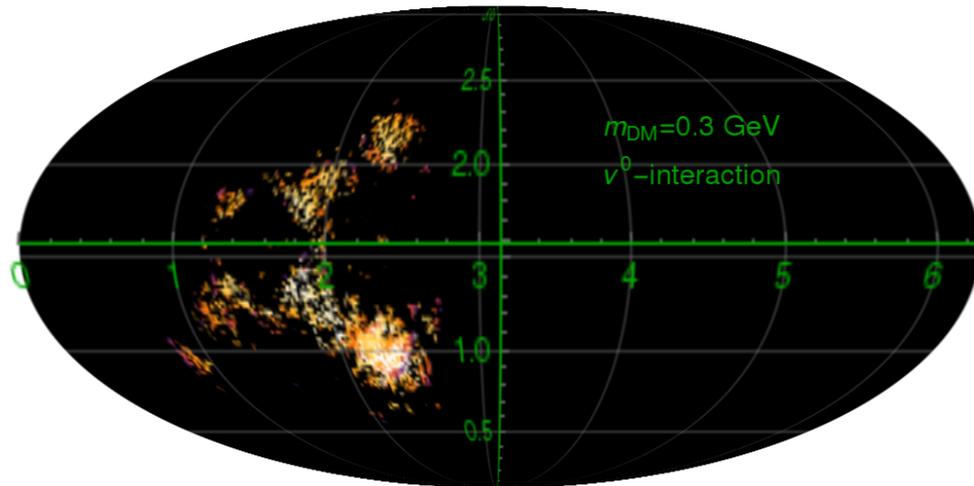
$E = 20 \text{ eV}$



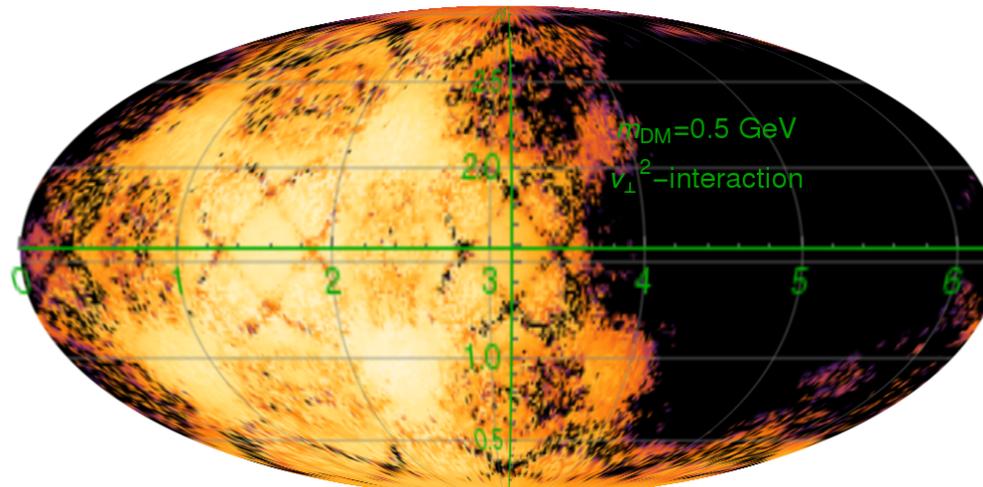
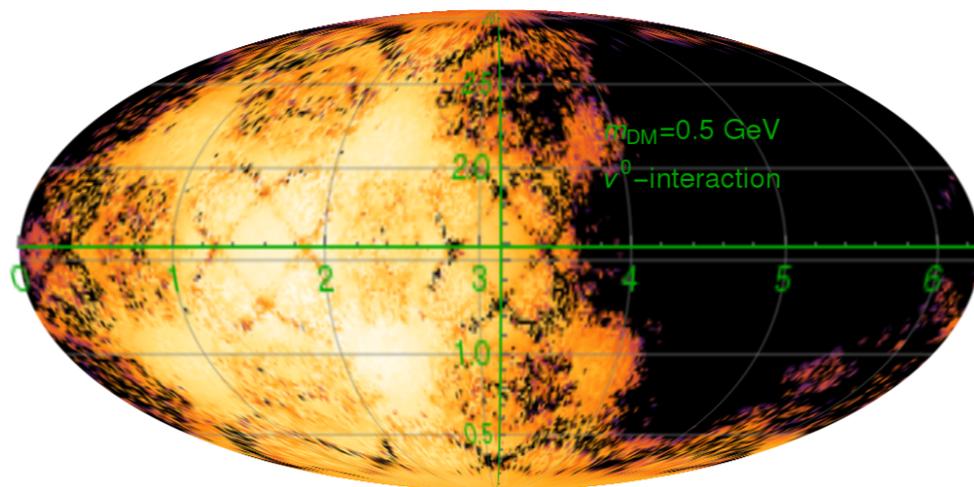
$$|\mathcal{M}|^2 \sim v^0$$

$$|\mathcal{M}|^2 \sim v_{\perp}^2$$

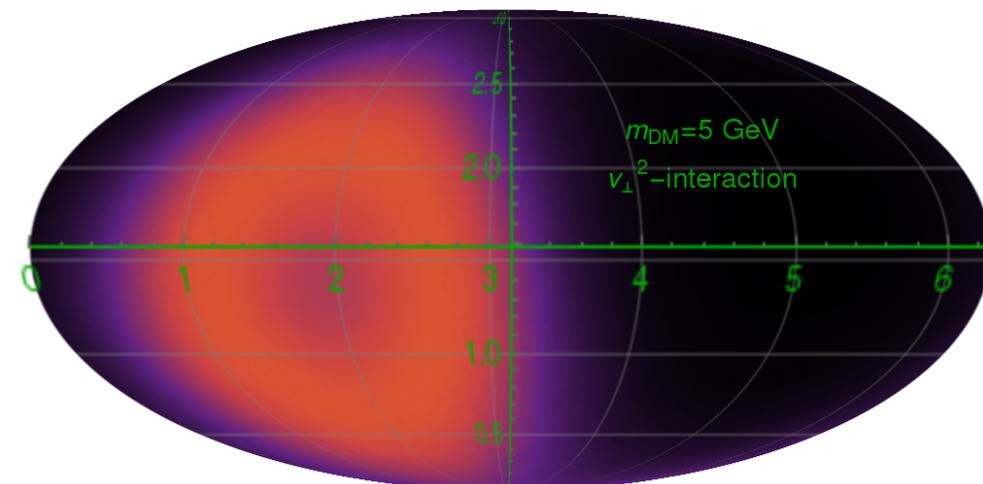
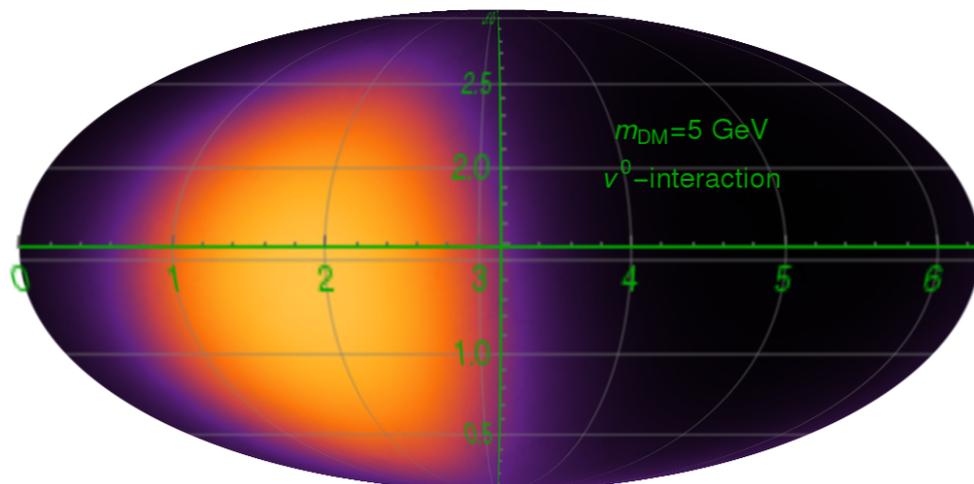
$m_{\text{DM}} = 0.3 \text{ GeV}$



$m_{\text{DM}} = 0.5 \text{ GeV}$

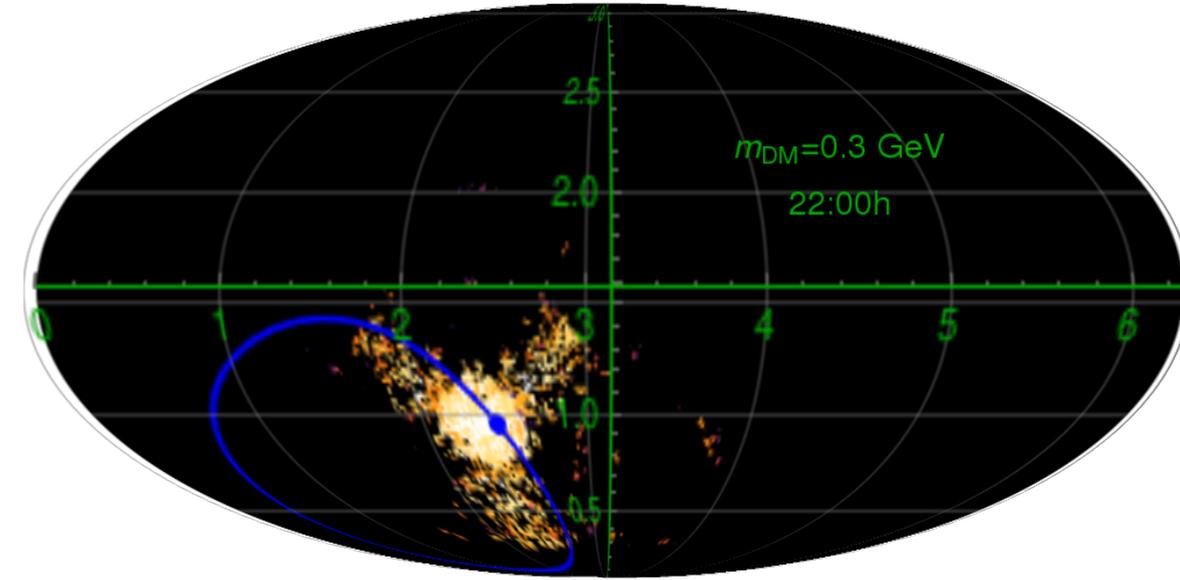
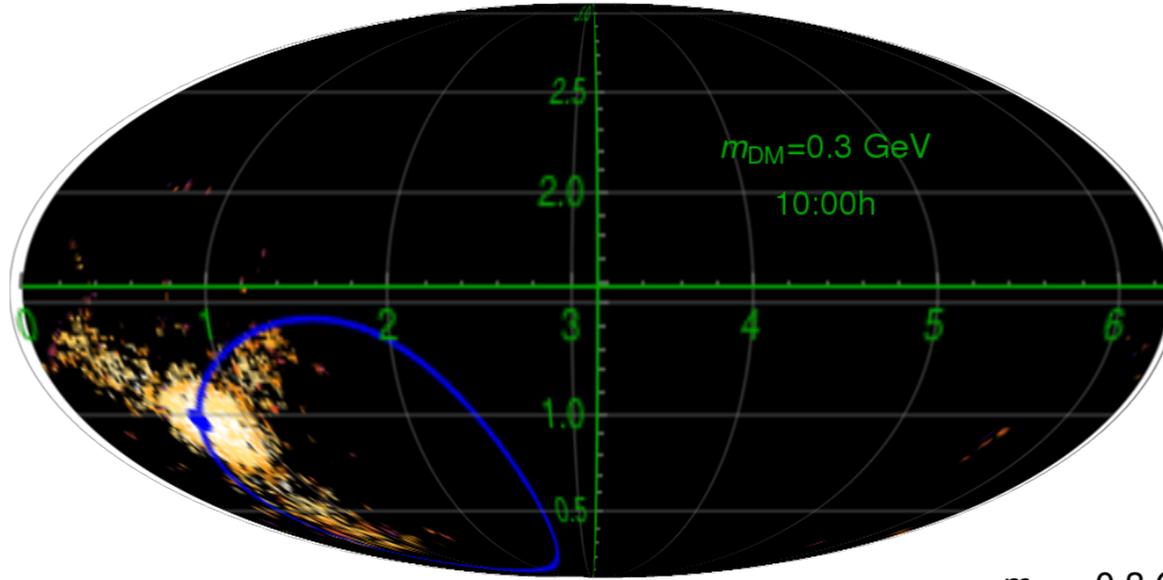


$m_{\text{DM}} = 5 \text{ GeV}$

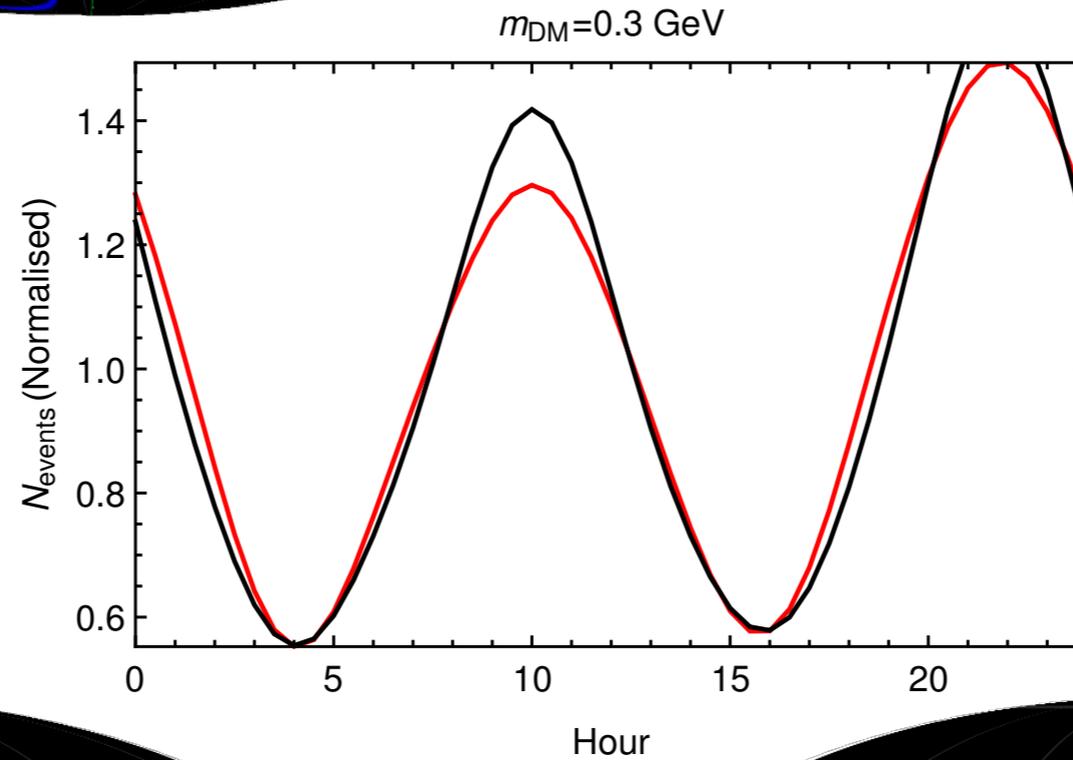


@SNOLAB, 6.9. at 18:00

The daily modulation

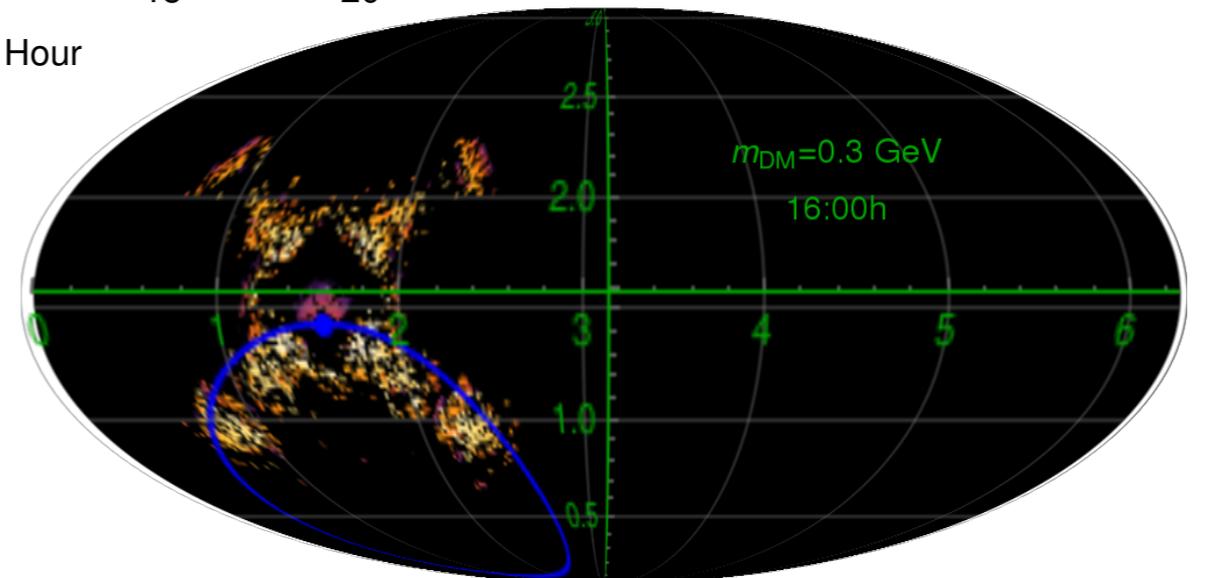
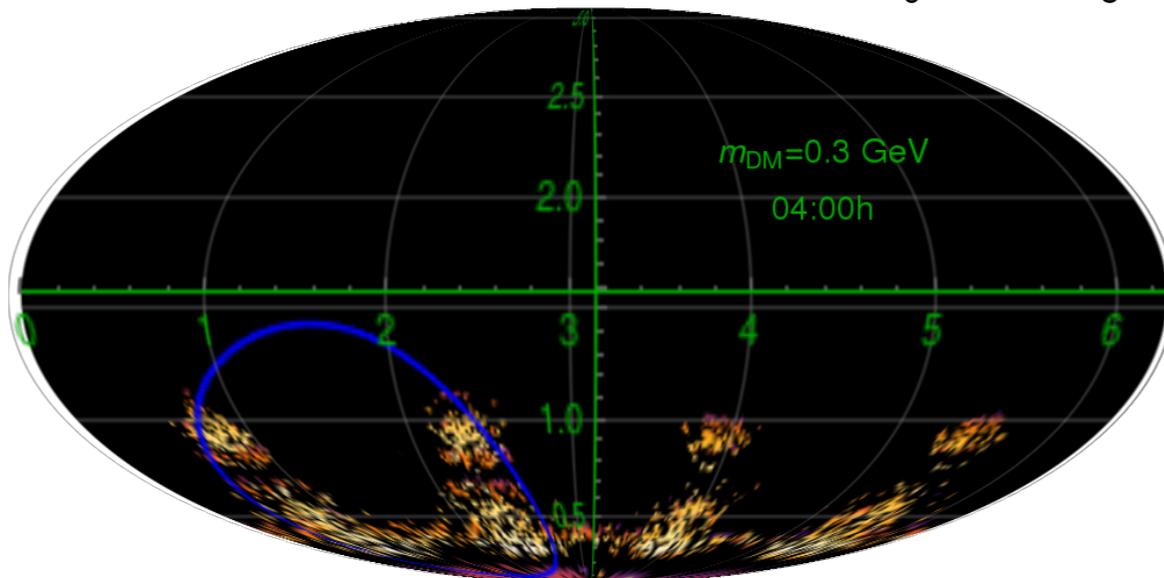


Total rate:

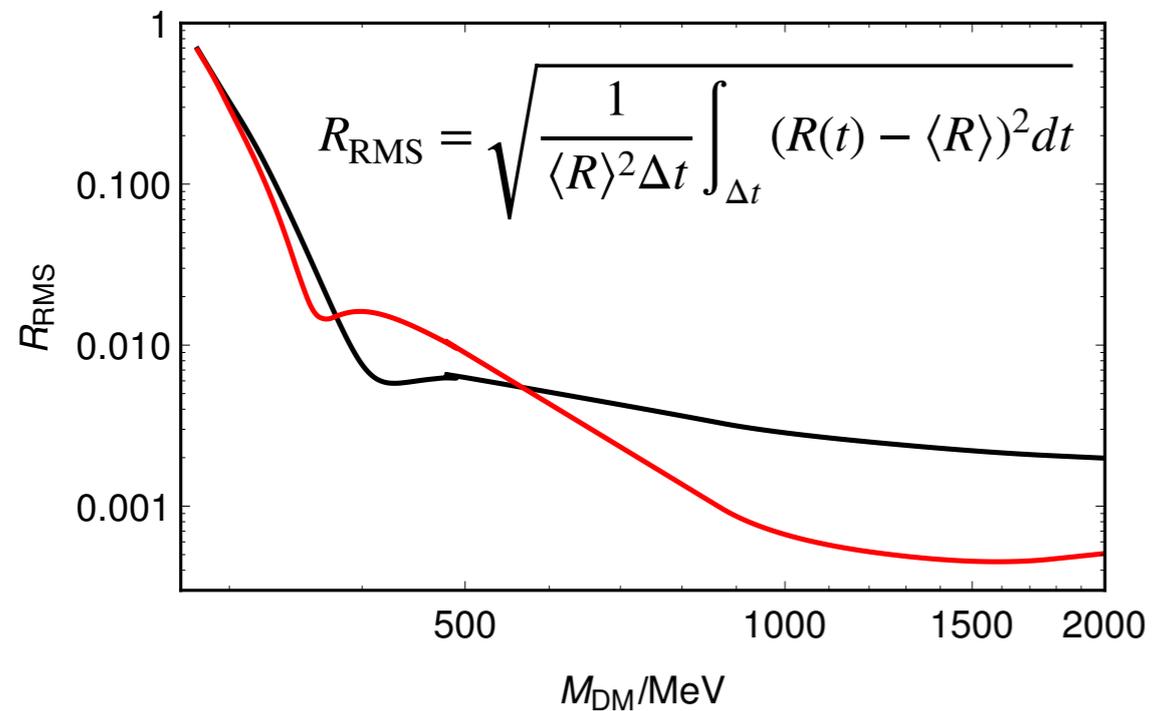
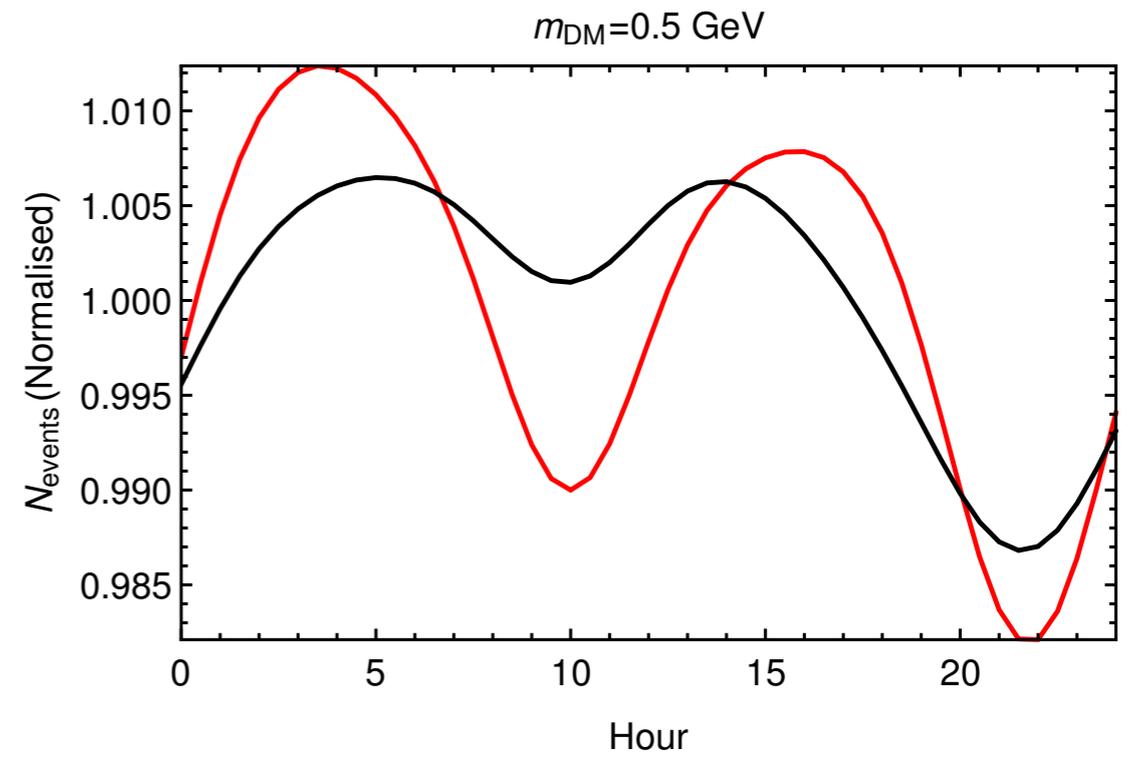
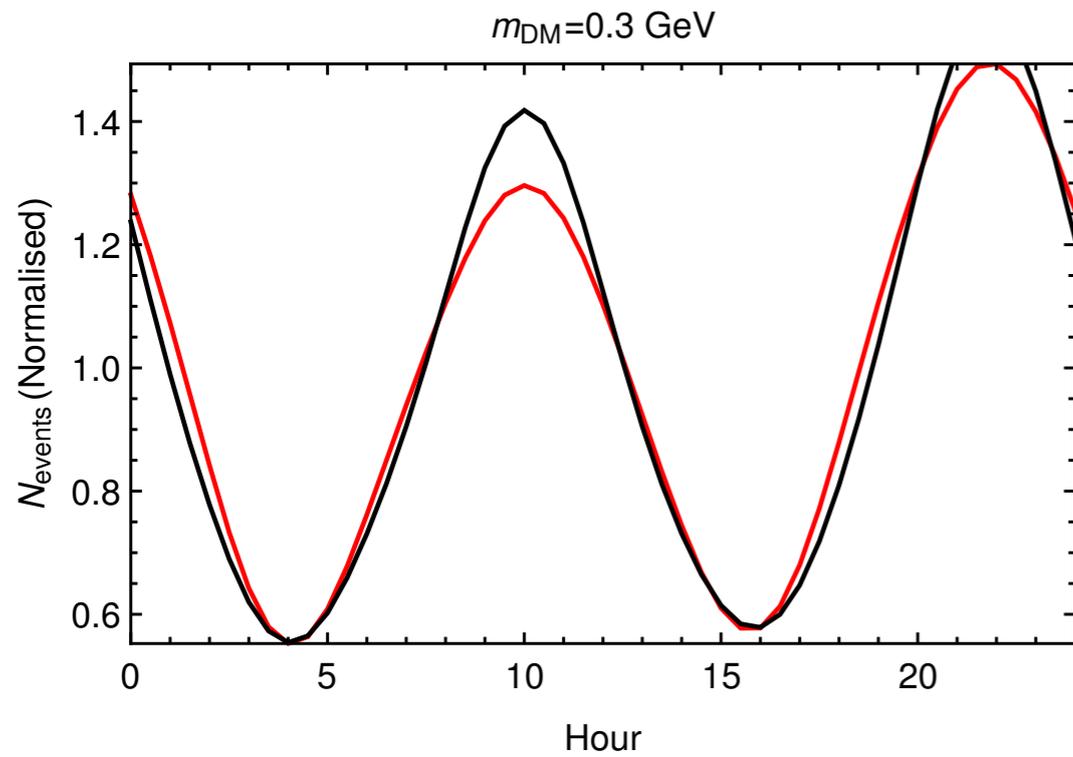


BLACK: $|\mathcal{M}|^2 \sim v^0$

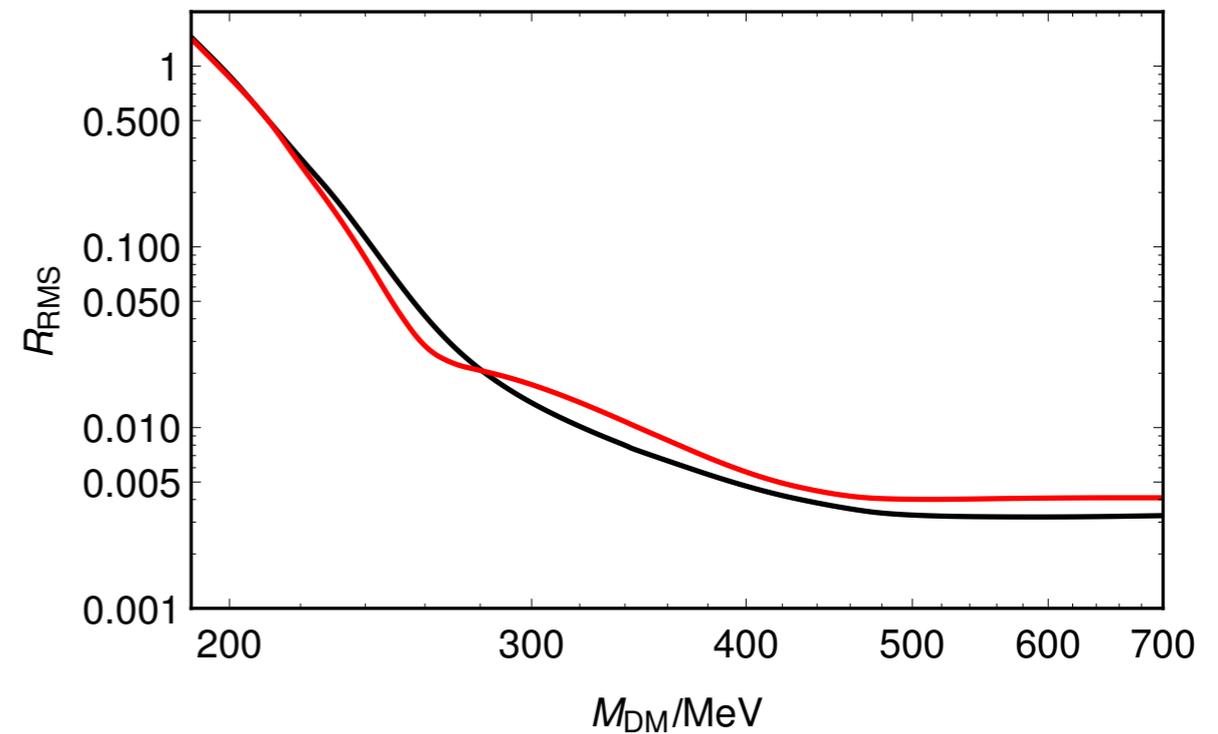
RED: $|\mathcal{M}|^2 \sim v^2$



Material dependent mass range of applicability



Germanium: $m_{\text{DM}} \leq 450 \text{ MeV}$



Silicon: $m_{\text{DM}} \leq 350 \text{ MeV}$

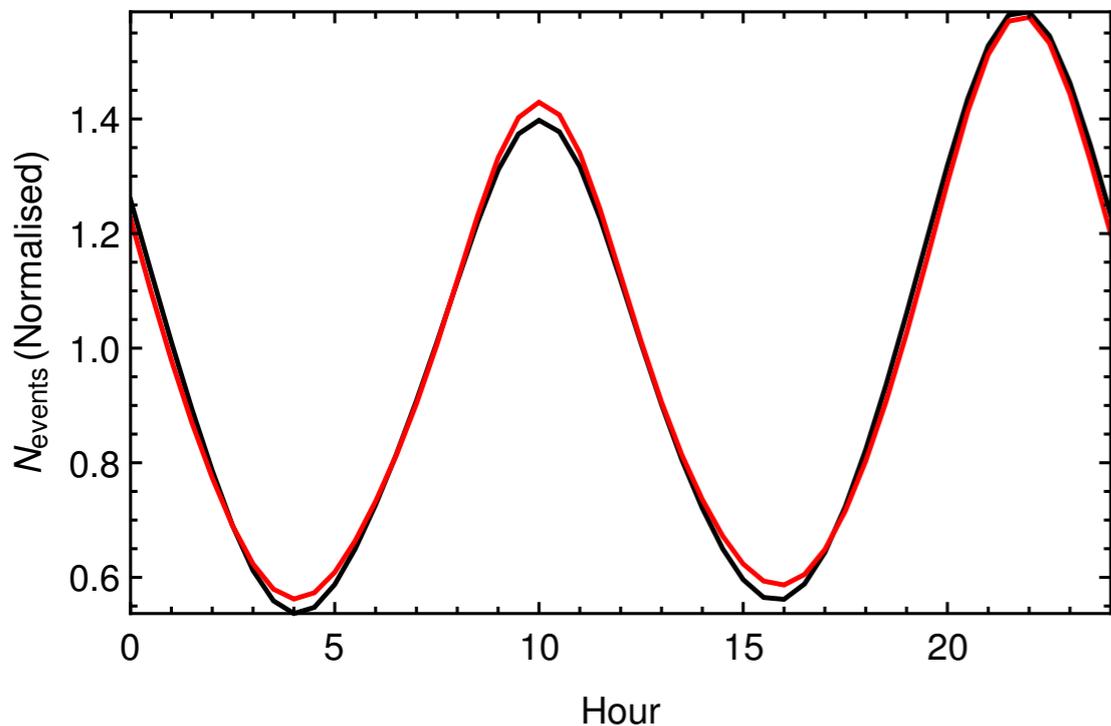
Energy dependent interactions:

$$|\mathcal{M}|^2 = a_1 1 + a_2 q^2 + a q^{-4} + \dots$$

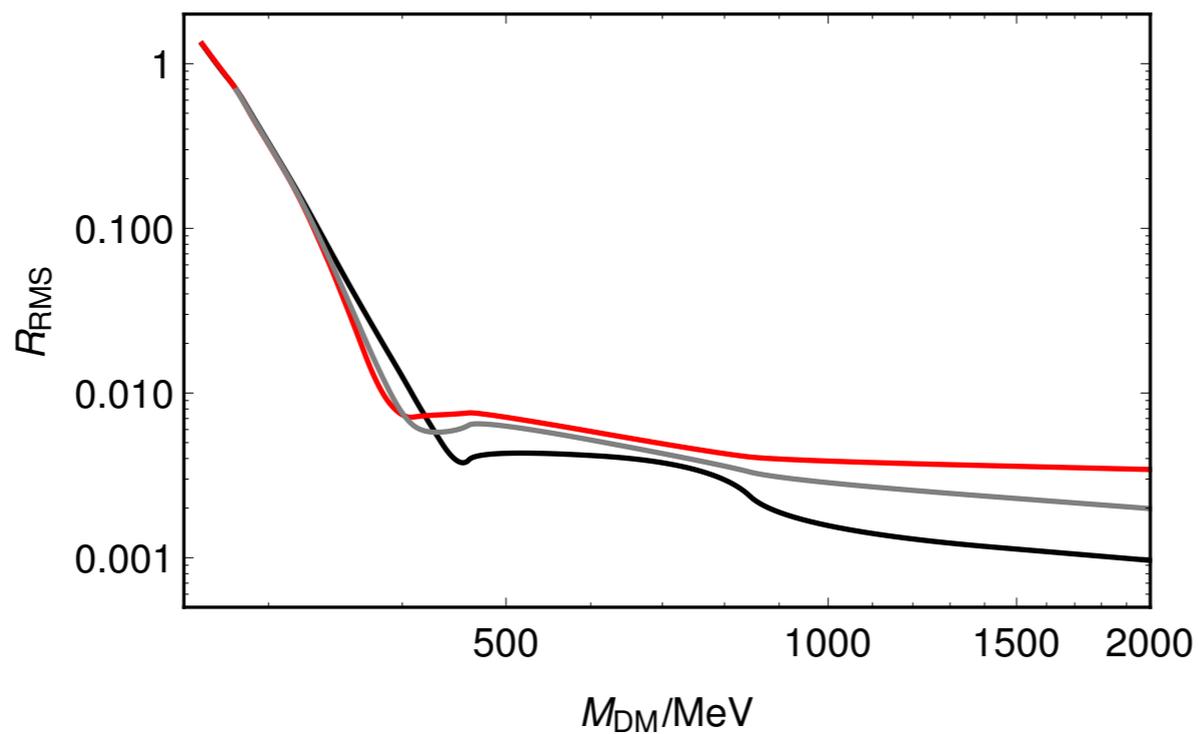
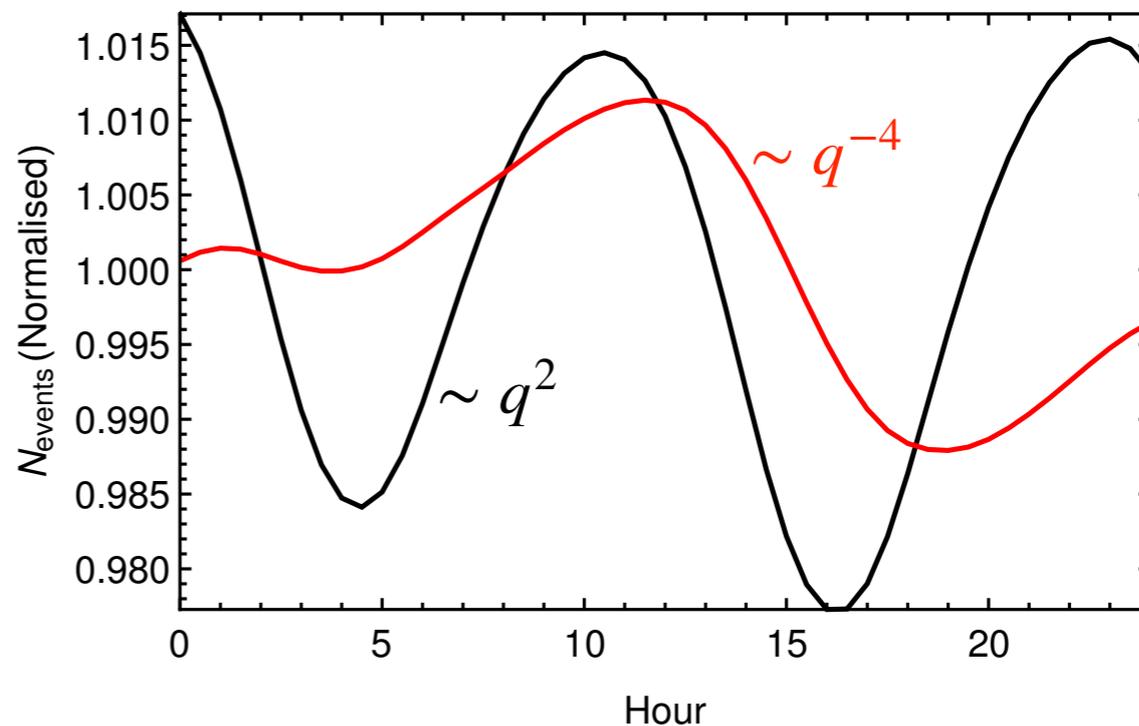
~~.....~~

Similar story:

$m_{\text{DM}}=0.3 \text{ GeV}$



$m_{\text{DM}}=0.4 \text{ GeV}$



3. Concluding remarks

Advantages and limitations

Advantages:

1. Modulation signals efficient in discriminating the origin of the signal.
2. The approach naturally works in the light dark matter regime.

Limitations:

1. Modulation only in a limited range in the light dark matter regime:
 - Lower E : no damage, no signal
 - Higher E : continuous signal, no benefit from threshold

Conclusion and outlook

Dark matter direct detection aiming to sub-GeV masses

Input for detector design by combining state-of-the-art computational materials physics and dark matter theory:

- Light dark matter provides a daily modulation signal in a semiconductor detector.
- Interactions with different velocity/energy dependence can lead to differences in the signal

Further work on neutrino background and dark matter velocity distributions in progress.