

1. Gaussian random variables

Give an example of a random vector $f = (f_1, f_2) : \Omega \rightarrow \mathbb{R}^2$, such that f_1 and f_2 are Gaussian, but the vector (f_1, f_2) is **not** Gaussian, i.e. there are some $a_1, a_2 \in \mathbb{R}$ such that $a_1 f_1 + a_2 f_2$ is not Gaussian.

2. Positive semi-definite

Proof that the function $\Gamma(s, t) := \min\{s, t\}$ is positive semi-definite.

3. From the lecture

Prove Theorem 1.7 using Theorem 1.6.

Hint: You might use the script 1a ...